

# **C28x IQmath Library**

**A Virtual Floating Point Engine**

**V1.5**

**July 8, 2008**

**Module user's Guide  
C28x Foundation Software**



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**Acronyms**

C28x+FPU: Refers to devices with the C28x plus floating-point-unit.

IQmath: High Accuracy Mathematical Functions (32-bit implementation).

QMATH: Fixed Point Mathematical computation

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# Chapter 1. Introduction

## 1.1. Introduction

Texas Instruments TMS320C28x IQmath Library is collection of highly optimized and high precision mathematical functions for C/C++ programmers to seamlessly port a floating-point algorithm into fixed point code on TMS320C28x devices. These routines are typically used in computationally intensive real-time applications where optimal execution speed and high accuracy is critical. By using these routines you can achieve execution speeds considerable faster than equivalent code written in standard ANSI C language. In addition, by providing ready-to-use high precision functions, TI IQmath library can shorten significantly your DSP application development time.

# Chapter 2. Installing the IQmath Library

## 2.1. IQmath Package Contents

The TI IQmath library can be used in both C and C++ programs and it consists of 5 parts:

- 1) The IQmath header files  
The header files include the definitions needed to interface with the IQmath library.  
C programs use IQmathLib.h
  - a) C++ programs use both IQmathLib.h and IQmathCPP.h
- 2) The IQmath object library. The library contains all of the IQmath functions and look-up tables. There are two builds of the library:
  - a) IQmath.lib: This build of the library can be linked with code built for fixed-point.
  - b) IQmath\_f32.lib: This build of the library can be linked with code built with the --float\_support=fpu32 switch. This can be useful for mixing IQmath with native floating-point code on devices with the C28x+FPU.
- 3) Example linker command files. The example linker command files allocate the sections used by the IQmath library. For some sections the location is device specific. For example, the tables used by the IQsin and IQcos functions are located within the boot ROM of the device.
- 4) IQmath GEL file. These gel functions are useful when using a version of Code Composer Studio that does not support IQ data types directly.
- 5) Example programs

## 2.2. How to Install the IQmath Library

The IQmath library is distributed in the form of a self-extracting ZIP file. By default, the install restores the IQmath library individual components in the directory structure shown below.

### NOTE:

**The directory structure of previous versions differed from what is shown below. For this release it has been reorganized to reduce duplication of files.**

<base> install directory is C:\tidcs\c28x\IQmath\v15

<base>\doc	Contains this file
<base>\include	The IQmath header files C code uses IQmathLib.h C++ code uses IQmathLib.h and IQmathCPP.h
<base>\lib	The IQmath library files. These are used by both C and C++ Refer to Chapter 4.
<base>\gel	Legacy GEL file for debug Refer to section 3.8.
<base>\examples\cmd	Linker command files used by the examples
<base>\examples\C	C example: Refer to ReadMe_SampleC.txt
<base>\examples\C\projects	CCS projects for the C example
<base>\examples\C\source	Source code for the C example
<base>\examples\Cpp	C++ code example: Refer to ReadMe_SampleCpp.txt
<base>\examples\Cpp\projects	CCS projects for the C++ example
<base>\examples\Cpp\source	Source code for the C++ example



# Chapter 3. Using the IQmath Library

## 3.1. IQmath Arguments and Data Types

Input/output of the IQmath functions are typically 32-bit fixed-point numbers and the Q format of the fixed-point number can vary from Q1 to Q30.

We have used typedefs to create aliases for IQ data types. This facilitates the user to define the variable of IQmath data type in the application program.

```
typedef long    _iq;      /* Fixed point data type: GLOBAL_Q format */
typedef long    _iq30;    /* Fixed point data type: Q30 format      */
typedef long    _iq29;    /* Fixed point data type: Q29 format      */
typedef long    _iq28;    /* Fixed point data type: Q28 format      */
typedef long    _iq27;    /* Fixed point data type: Q27 format      */
typedef long    _iq26;    /* Fixed point data type: Q26 format      */
typedef long    _iq25;    /* Fixed point data type: Q25 format      */
typedef long    _iq24;    /* Fixed point data type: Q24 format      */
typedef long    _iq23;    /* Fixed point data type: Q23 format      */
typedef long    _iq22;    /* Fixed point data type: Q22 format      */
typedef long    _iq21;    /* Fixed point data type: Q21 format      */
typedef long    _iq20;    /* Fixed point data type: Q20 format      */
typedef long    _iq19;    /* Fixed point data type: Q19 format      */
typedef long    _iq18;    /* Fixed point data type: Q18 format      */
typedef long    _iq17;    /* Fixed point data type: Q17 format      */
typedef long    _iq16;    /* Fixed point data type: Q16 format      */
typedef long    _iq15;    /* Fixed point data type: Q15 format      */
typedef long    _iq14;    /* Fixed point data type: Q14 format      */
typedef long    _iq13;    /* Fixed point data type: Q13 format      */
typedef long    _iq12;    /* Fixed point data type: Q12 format      */
typedef long    _iq11;    /* Fixed point data type: Q11 format      */
typedef long    _iq10;    /* Fixed point data type: Q10 format      */
typedef long    _iq9;     /* Fixed point data type: Q9 format       */
typedef long    _iq8;     /* Fixed point data type: Q8 format       */
typedef long    _iq7;     /* Fixed point data type: Q7 format       */
typedef long    _iq6;     /* Fixed point data type: Q6 format       */
typedef long    _iq5;     /* Fixed point data type: Q5 format       */
typedef long    _iq4;     /* Fixed point data type: Q4 format       */
typedef long    _iq3;     /* Fixed point data type: Q3 format       */
typedef long    _iq2;     /* Fixed point data type: Q2 format       */
typedef long    _iq1;     /* Fixed point data type: Q1 format       */
```

### 3.2. IQmath Data type: Range & Resolution

Following table summarizes the Range & Resolution of 32-bit fixed-point number for different Q format representation. Typically IQmath function supports Q1 to Q30 format, nevertheless some functions like IQNsin, IQNcos, IQNatan2, IQNatan2PU, IQatan do not support Q30 format, due to the fact that these functions input or output vary between  $-\pi$  to  $\pi$  radians.

Data Type	Range		Resolution/Precision
	Min	Max	
_iq30	-2	1.999 999 999	0.000 000 001
_iq29	-4	3.999 999 998	0.000 000 002
_iq28	-8	7.999 999 996	0.000 000 004
_iq27	-16	15.999 999 993	0.000 000 007
_iq26	-32	31.999 999 985	0.000 000 015
_iq25	-64	63.999 999 970	0.000 000 030
_iq24	-128	127.999 999 940	0.000 000 060
_iq23	-256	255.999 999 981	0.000 000 119
_iq22	-512	511.999 999 762	0.000 000 238
_iq21	-1024	1023.999 999 523	0.000 000 477
_iq20	-2048	2047.999 999 046	0.000 000 954
_iq19	-4096	4095.999 998 093	0.000 001 907
_iq18	-8192	8191.999 996 185	0.000 003 815
_iq17	-16384	16383.999 992 371	0.000 007 629
_iq16	-32768	32767.999 984 741	0.000 015 259
_iq15	-65536	65535.999 969 482	0.000 030 518
_iq14	-131072	131071.999 938 965	0.000 061 035
_iq13	-262144	262143.999 877 930	0.000 122 070
_iq12	-524288	524287.999 755 859	0.000 244 141
_iq11	-1048576	1048575.999 511 719	0.000 488 281
_iq10	-2097152	2097151.999 023 437	0.000 976 563
_iq9	-4194304	4194303.998 046 875	0.001 953 125
_iq8	-8388608	8388607.996 093 750	0.003 906 250
_iq7	-16777216	16777215.992 187 500	0.007 812 500
_iq6	-33554432	33554431.984 375 000	0.015 625 000
_iq5	-67108864	67108863.968 750 000	0.031 250 000
_iq4	-134217728	134217727.937 500 000	0.062 500 000
_iq3	-268435456	268435455.875 000 000	0.125 000 000
_iq2	-536870912	536870911.750 000 000	0.250 000 000
_iq1	-1073741824	1 073741823.500 000 000	0.500 000 000

### 3.3. Calling an IQmath Function from C

In addition to installing the IQmath software, to include an IQmath function in your code you have to:

- Include the IQmathLib.h include file
- Link your code with the IQmath object code library. This will normally be the IQmath.lib library. If you have a C28x with floating-point device and wish to mix IQmath and native floating-point, then use the IQmath\_fpu32.lib. This file contains all of the IQmath functions in object format. The library is constructed such that ONLY the functions that are used are included as part of the project. This minimizes code size.
- The linker command file should be updated to properly access the IQmath lookup tables and place the IQmath code in the memory block you wish. These sections are described later in this chapter.
- Call the functions using the `_iq` and `_iqN` data types along with the C-code function definitions. For example, the following code contains a call to the ***IQ25sin*** routines in IQmath Library:

```
#include<IQmathLib.h>
#define PI 3.14159

_iq input, sin_out;
void main(void )
{
    /* 0.25 x PI radians represented in Q29 format          */
    input=_IQ29(0.25*PI);
    sin_out =_IQ29sin(input);
}
```

### 3.4. Calling an IQmath function from C++

In C++ the `_iq` type becomes the `iq` class. This allows for function overloading of operators such as multiply and divide. To access the library from C++ follow these steps:

- Include both the IQmathLib.h and the IQmathCPP.h header file as shown below:

```
extern "C" {
#include "IQmathLib.h"
}
#include "IQmathCPP.h"
```

- Link your code with the IQmath object code library. This will normally be the IQmath.lib library. If you have a C28x with floating-point device and wish to mix IQmath and native floating-point, then use the IQmath\_fpu32.lib. Notice the same library is used by both C and C++ code. This file contains all of the IQmath functions in object format. The library is constructed such that ONLY the functions that are used are included as part of the project. This minimizes code size.
- The linker command file should be updated to properly access the IQmath lookup tables and place the IQmath code in the memory block you wish. These sections are described later in this chapter.

- Call the functions using the iq and iqN classes along with the C++ code function definitions. In C++ the functions are called without the leading underscore and the math operations are overloaded. For example:

C Code	C++ Code	Note
<code>_iq, _iqN</code>	<code>iq, iqN</code>	IQ Data Types
<code>_IQ(A), _IQN(A)</code>	<code>IQ(A), IQN(A)</code>	Convert float to IQ
<code>_IQdiv(A,B)</code>	<code>A/B</code>	Division

The following example code contains a call to the ***IQ25sin*** routines in IQmath Library using C++ code:

```
extern "C" {
#include "IQmathLib.h"
}
#include "IQmathCPP.h"
#define PI 3.14159

iq input, sin_out;
void main(void )
{
    /* 0.25 x PI radians represented in Q29 format */
    input = IQ29(0.25*PI);
    sin_out = IQ29sin(input);
}
```

### 3.5. IQmath Section and Lookup Tables

Some of the IQmath functions use look-up tables. Many of these tables are included in the boot ROM of 28x devices. Using the boot ROM copy will save you memory space and the time required to load the tables themselves. Note that the boot ROM on most devices is 1 wait state compared to SARAM that is usually 0 wait state. The look-up tables are usually not accessed often enough for this to cause an issue with performance. Therefore, in most cases you will want to use the boot ROM look-up tables.

The IQmath library uses the following lookup tables:

#### **IQmathTables:**

This section contains look-up tables for the most often used IQmath functions. This includes IQdiv, IQsin, IQcos, IQsqrt and IQatan2. The IQmathTables are available in the boot ROM of all 28x devices. Hence, this section should be identified as a "NOLOAD" type in the linker command file. This facilitates referencing look-up table symbols without actually loading the section into the target.

#### **IQmathTablesRam:**

This section contains look-up tables used by the IQexp, IQasin and IQacos functions. If you do not call these functions, then there is no need to load this section. Some devices also include some of these tables in the boot ROM as shown in the following table.

Device	Table	Boot ROM Location
281x	IQmathTables	0x3FF000
280x	IQmathTables	0x3FF000
2801x	IQmathTables	0x3FF000
2833x/2823x	IQmathTables	0x3FE000
	IQmathTablesRam (IQNexpTable.obj only)	0x3FEB50

If your device is not listed, refer to the boot ROM reference guide and the boot ROM source code for your device to get more information.

If a table is not included in the boot ROM of the device, then it must be loaded into the appropriate memory in the linker command file.

The following is an example of a linker file for the 281x devices. In this case only the IQmathTables section is in the boot ROM. If used, the IQmathTablesRam section must be loaded into the device along with the application itself.

IQmath Linker Command File Example: 281x Devices	
<pre> MEMORY {   PAGE 0:     PRAMH0 (RW)      : origin = 0x3f8000, length = 0x001000   PAGE 1:     IQTABLES (R)      : origin = 0x3FF000, length = 0x000b50     DRAMH0 (RW)      : origin = 0x3f9000, length = 0x001000 } SECTIONS {   IQmathTables      : load = IQTABLES, type = NOLOAD, PAGE = 1   IQmathTablesRam   : load = DRAMH0, PAGE = 1   IQmath            : load = PRAMH0, PAGE = 0 } </pre>	

The 2833x and 2823x boot ROM includes the IQNexpTable used by the IQNexp() and IQexp() functions. In this case the IQNexpTable can be placed into its own section and identified as type NOLOAD as shown in the next example. The remainder of the IQmathTablesRam section is allocated to SARAM.

It should be noted that if the IQexp() or IQNexp() function is not called in the application, then the allocation for IQNexpTable.obj will result in a linker warning. This is because the table will not be included if it is not used. This warning will not cause any ill effects to the normal operation of the application.

### IQmath Linker Command File Example: 2823x Device

```
MEMORY
{
  PAGE 0:
    PRAML0 (RW)      : origin = 0x008000, length = 0x001000
  PAGE 1:
    IQTABLES (R)      : origin = 0x3FE000, length = 0x000b50
    IQTABLES2 (R)     : origin = 0x3FEB50, length = 0x00008c
    DRAML1 (RW)      : origin = 0x009000, length = 0x001000
}
SECTIONS
{
  IQmathTables      : load = IQTABLES, type = NOLOAD, PAGE = 1
  IQmathTables2 > IQTABLES2, type = NOLOAD, PAGE = 1
  {
    IQmath.lib<IQNexpTable.obj> (IQmathTablesRam)
  }
  IQmathTablesRam : load = DRAML1, PAGE = 1
  IQmath          : load = PRAML0, PAGE = 0
}
```

### 3.6. IQmath Naming Conventions

Each IQmath function comes in two types as shown below:

- ❑ GLOBAL\_Q function, that takes input/output in GLOBAL\_Q format

C-Code Examples:

```

• _IQsin(A)           /* High Precision SIN           */
• _IQcos(A)           /* High Precision COS           */
• _IQrmpy(A,B)        /* IQ multiply with rounding    */
• _IQmpy(A,B)         /* IQ multiply                  */

```

C++ Code Examples:

```

• IQsin(A)            /* High Precision SIN           */
• IQcos(A)            /* High Precision COS           */
• IQrmpy(A,B)         /* IQ multiply with rounding    */
• A*B                 /* IQ multiply                  */

```

- ❑ Q-format specific functions to cater to Q1 to Q30 data format.

C-Code Examples:

```

• _IQ29sin(A)         /* High Precision SIN: input/output are in Q29 */
• _IQ28sin(A)         /* High Precision SIN: input/output are in Q28 */
• _IQ27sin(A)         /* High Precision SIN: input/output are in Q27 */
• _IQ26sin(A)         /* High Precision SIN: input/output are in Q26 */
• _IQ25sin(A)         /* High Precision SIN: input/output are in Q25 */
• _IQ24sin(A)         /* High Precision SIN: input/output are in Q24 */

```

C++ Code Examples:

```

• IQ29sin(A)          /* High Precision SIN: input/output are in Q29 */
• IQ28sin(A)          /* High Precision SIN: input/output are in Q28 */
• IQ27sin(A)          /* High Precision SIN: input/output are in Q27 */
• IQ26sin(A)          /* High Precision SIN: input/output are in Q26 */
• IQ25sin(A)          /* High Precision SIN: input/output are in Q25 */
• IQ24sin(A)          /* High Precision SIN: input/output are in Q24 */

```

IQmath C Function Naming Convention	
GLOBAL_Q Function	
<b>_IQXXX( )</b> , Where “XXX” is the Function Name	
Q Specific Function	
<b>_IQNXXX( )</b> , Where “XXX” is the Function Name & “N” is the Q format of input/output	

### 3.7. Selecting the GLOBAL\_Q format

Numerical precision and dynamic range requirement will vary considerably from one application to other. IQmath Library facilitates the application programming in fixed-point arithmetic, without fixing the numerical precision up-front. This allows the system engineer to check the application performance with different numerical precision and finally fix the numerical resolution. As explained in section 3.2, higher the precision results in lower dynamic range. Hence, the system designer must trade-off between the range and resolution before choosing the GLOBAL\_Q format.

#### CASE I:

Default GLOBAL\_Q format is set to Q24. Edit "IQmathLib.h" header file to modify this value as required, user can choose from Q1 to Q29 as GLOBAL\_Q format. Modifying this value means that all the GLOBAL\_Q functions will use this Q format for input/output, unless this symbolic definition is overridden in the source code.

IQmathLib.h : Selecting GLOBAL_Q format				
#ifndef	GLOBAL_Q			
#define	GLOBAL_Q	24	/* Q1 to Q29	*/
#endif				

#### CASE II :

A complete system consists of various modules. Some modules may require different precision, then the rest of the system. In such situation, we need to over-ride the GLOBAL\_Q defined in the "IQmathLib.h" file and use the local Q format.

This can be easily done by defining the GLOBAL\_Q constant in the source file of the module before the include statement.

MODULE6.C : Selecting Local Q format				
#define	GLOBAL_Q	27	/* Set the Local Q value	*/
#include	<IQmathLib.h>			



### 3.8. Using the IQmath GEL file for Debugging

**This information is useful when using an older version of Code Composer Studio that does not support IQ data types directly.**

IQmath GEL file contains GEL functions that helps to view IQ variables in watch window and allows the setting of IQ variable values via dialogue boxes.

#### Step 1: Define “GlobalQ” variable

In one of the user source file, the following global variable must be defined:

```
long GlobalQ = GLOBAL_Q;
```

This variable is used by the GEL functions to determine the current GLOBAL\_Q setting.

#### Step 2: Load GEL file

Load the "IQmath.gel" file into the user project. This will automatically load a set of GEL functions for displaying IQ variables in the watch window and create the following menus under the GEL toolbar

- IQ C Support
- IQ C++ Support

#### Step 3: Viewing IQmath variable

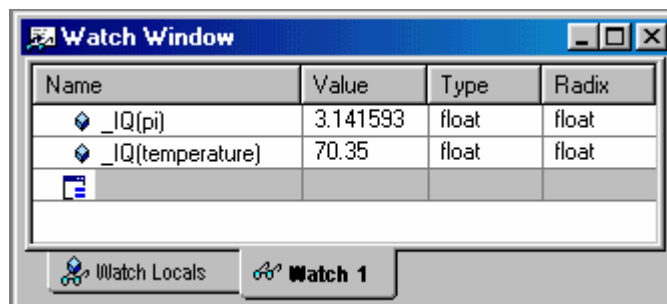
To view a variable in the watch window, simply type the following commands in the watch window. They will convert the specified "VarName" in IQ format to the equivalent floating-point value:

For C variables:

```
_IQ(VarName)      ; GLOBAL_Q value  
_IQN(VarName)     ; N = 1 to 30
```

For C++ variables:

```
IQ(VarName)       ; GLOBAL_Q value  
IQN(VarName)      ; N = 1 to 30
```

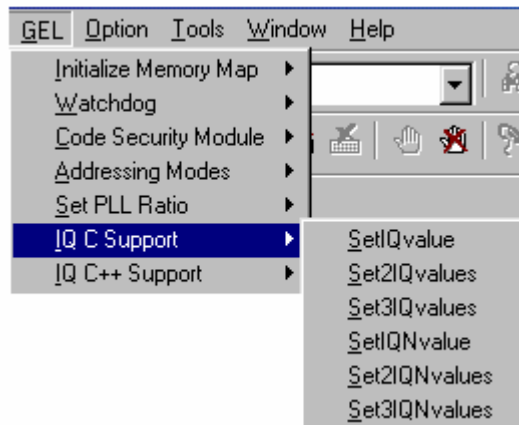


#### Step 4: Modifying IQmath variable

The watch window does not allow the modification of variables that are not of native type. To facilitate this, the following GEL operations can be found under the GEL toolbar:

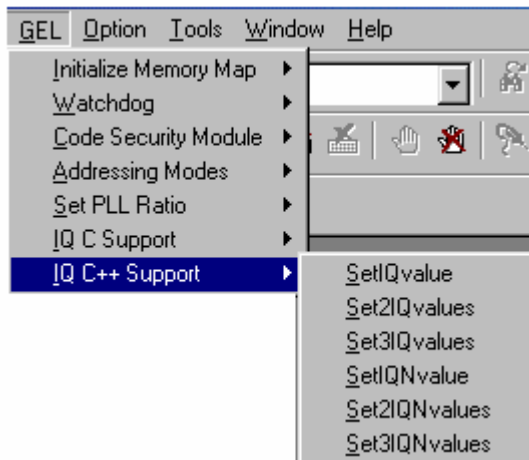
##### **IQ C Support**

- SetIQvalue ; GLOBAL\_Q format
- Set2IQvalues
- Set3IQvalues
- SetIQNvalue ; IQN format
- Set2IQNvalues
- Set3IQNvalues



##### **IQ C++ Support**

- SetIQvalue ; GLOBAL\_Q format
- Set2IQvalues
- Set3IQvalues
- SetIQNvalue ; IQN format
- Set2IQNvalues
- Set3IQNvalues



Invoking one of the above GEL operations will bring up a dialogue box window, which the user can enter the variable name and the floating-point value to set. The function will convert the float value to the appropriate IQ value.

### 3.9. Converting an IQmath Application to Floating-Point

To convert an IQmath application to floating point, follow these steps:

1. In the IQmath header file, select `FLOAT_MATH`. The header file will convert all IQmath function calls to their floating-point equivalent.
2. When writing a floating-point number into a device register, you need to convert the floating-point number to an integer. Likewise when reading a value from a register it will need to be converted to float. In both cases, this is done by multiplying the number by a conversion factor.

For example to convert a floating-point number to IQ15, multiply by 32768.0.

```
#if MATH_TYPE == IQ_MATH
    PwmReg = (int16)_IQtoIQ15(Var1);
#else // MATH_TYPE is FLOAT_MATH
    PwmReg = (int16)(32768.0L*Var1);
#endif
```

Likewise, to convert from an IQ15 value to a floating-point value, multiply by 1/32768.0 or 0.000030518.0.

Note: The integer range is restricted to 24-bits for a 32-bit floating-point value.

3. If your device has the on-chip floating-point processing unit (C28x+FPU), then you can take advantage of the on-chip floating point unit by doing the following:
  - Use C28x codegen tools version 5.0.2 or later.
  - Tell the compiler it can generate native C28x floating-point code. To do this, use the `-v28 --float_support=fpu32` compiler switches. In Code Composer Studio the `float_support` switch is on the advanced tab of the compiler options.
  - Use the correct run-time support library for native 32-bit floating-point. For C code this is `rts2800_fpu32.lib`. For C++ code with exception handling, use `rts2800_fpu32_eh.lib`.
  - Use the C28x FPU Fast RTS library (SPRC664) to get a performance boost from math functions such as `sin`, `cos`, `div`, `sqrt`, and `atan`. The Fast RTS library should be linked in before the normal run-time support library.

### 3.10. The IQmath C-Calling Convention

All of the IQmath functions strictly adhere to the C28x C-Calling conventions. To understand the C28x C-Calling convention, Please refer Chapter 7 (Run-time Environment) of TMC320C28x Optimizing C/C++ Compiler User's Guide (SPRU514).

# Chapter 4. Libraries Available

This chapter lists the builds available for the IQmath source.

- **IQmath.lib**

The IQmath.lib library has been built for use on standard C28x fixed-point devices. This library can be used with both C and C++ code.

- **IQmath\_fpu32.lib**

The IQmath\_fpu32.lib library is useful for users who want to use both IQmath functions as well as native C28x floating-point code within their project. This library can be used with both C and C++ code.

The IQmath\_fpu32.lib library has been built with the following compiler flags:

`-v28 --float_support=fpu32`

IQmath\_fpu32.lib still contains the same IQmath functions as IQmath.lib. It does not contain native floating-point functions. The float\_support option is available in the C28x compiler version 5.0.0 and later.

# Chapter 5. Function Summary

The routines included within the IQmath library are organized as follows

- ❑ Format conversion utilities : atolQ, IQtoF, IQtoIQN etc.
- ❑ Arithmetic Functions : IQmpy, IQdiv etc.
- ❑ Trigonometric Functions : IQsin, IQcos, IQatan2 etc.
- ❑ Mathematical functions : IQsqrt, IQisqrt etc.
- ❑ Miscellaneous : IQabs, IQsat etc

## 5.1. Arguments and Conventions Used

The following convention has been followed when describing the arguments for each individual function:

QN	16-bit fixed point Q number, where N=1:15
IQN	32-bit fixed point Q number, where N=1:31
int	16-bit number
long	32-bit number
_iq	<p>_iq is the C-code data type definition equating a long, a 32-bit value representing a GLOBAL_Q number. Usage of _iq instead of long is recommended to increase future portability across devices.</p> <p>For C++ code the iq class is used instead.</p>
_iqN	<p>_iqN is the C-code data type definition equating a long, a 32-bit value representing a IQN number, where N=1:30</p> <p>For C++ code, the iqN class is used instead.</p>
iq	C++ iq class for handling the _iq data type.
iqN	C++ iqN class for handling the _iqN data type.
A, B	Input operand to IQmath function or Macro
F	Floating point input : Ex: -1.232, +22.433, 0.4343, -0.32
S	Floating point string: "+1.32", "0.232", "-2.343" etc
P	Positive Saturation value
N	Negative Saturation value

## 5.2. IQmath Function Overview

### Format conversion Utilities

Functions	Description	IQ format
_iq _IQ(float F) _iqN _IQN(float F)	Converts float to IQ value	Q=GLOBAL_Q Q=1:30
float _IQtoF( _iq A) float _IQNtoF( _iqN A)	IQ to Floating point	Q=GLOBAL_Q Q=1:30
_iq _atolQ( char *S) _iqN _atolQN( char *S)	Float ASCII string to IQ	Q=GLOBAL_Q Q=1:30
int _IQtoa(char *S, const * format, long x) int _IQNtoa(char *S, const * format, long x)	IQ to ASCII string	Q=GLOBAL_Q Q=1:30
long _IQint( _iq A) long _IQNint( _iqN A)	extract integer portion of IQ	Q=GLOBAL_Q Q=1:30
_iq _IQfrac( _iq A) _iqN _IQNfrac( _iqN A)	extract fractional portion of IQ	Q=GLOBAL_Q Q=1:30
_iqN _IQtoIQN( _iq A)	Convert IQ number to IQN number (32-bit)	Q=GLOBAL_Q
_iq _IQNtoIQ( _iqN A)	Convert IQN (32-bit) number to IQ number	Q=GLOBAL_Q
int _IQtoQN( _iq A)	Convert IQ number to QN number (16-bit)	Q=GLOBAL_Q
_iq _QNtoIQ( int A)	Convert QN (16-bit) number to IQ number	Q=GLOBAL_Q

### Arithmetic Operations

Functions	Description	IQ format
_iq _IQmpy( _iq A, _iq B) _iqN _IQNmpy( _iqN A, _iqN B)	IQ Multiplication	Q=GLOBAL_Q Q=1:30
_iq _IQrmpy( _iq A, _iq B) _iqN _IQNrmpy( _iqN A, _iqN B)	IQ Multiplication with rounding	Q=GLOBAL_Q Q=1:30
_iq _IQrsmpy( _iq A, _iq B) _iqN _IQNrsmpy( _iqN A, _iqN B)	IQ multiplication with rounding & saturation	Q=GLOBAL_Q Q=1:30
_iq _IQmpyI32( _iq A, long B) _iqN _IQNmpyI32( _iqN A, long B)	Multiply IQ with "long" integer	Q=GLOBAL_Q Q=1:30
long _IQmpyI32int( _iq A, long B) long _IQNmpyI32int( _iqN A, long B)	Multiply IQ with "long", return integer part	Q=GLOBAL_Q Q=1:30
long _IQmpyI32frac( _iq A, long B) long _IQNmpyI32frac( _iqN A, long B)	Multiply IQ with "long", return fraction part	Q=GLOBAL_Q Q=1:30
_iq _IQmpyIQX( _iqN1 A, N1, _iqN2 B, N2 ) _iqN _IQmpyIQX( _iqN1 A, N1, _iqN2 B, N2 )	Multiply two 2-different IQ number	Q=GLOBAL_Q Q=1:30
_iq _IQdiv( _iq A, _iq B) _iqN _IQNdiv( _iqN A, _iqN B)	Fixed point division	Q=GLOBAL_Q Q=1:30

**Trigonometric Functions:**

Functions	Description	IQ format
_iq _IQasin( _iq A) _iqN _IQNasin( _iqN A)	High precision ASIN (output in radians)	Q=GLOBAL_Q Q=1:29
_iq _IQsin( _iq A) _iqN _IQNsin( _iqN A)	High precision SIN (input in radians)	Q=GLOBAL_Q Q=1:29
_iq _IQsinPU( _iq A) _iqN _IQNsinPU( _iqN A)	High precision SIN (input in per-unit)	Q=GLOBAL_Q Q=1:30
_iq _IQacos( _iq A) _iqN _IQNacos( _iqN A)	High precision ACOS (output in radians)	Q=GLOBAL_Q Q=1:30
_iq _IQcos( _iq A) _iqN _IQNcos( _iqN A)	High precision COS (Input in radians)	Q=GLOBAL_Q Q=1:29
_iq _IQcosPU( _iq A) _iqN _IQNcosPU( _iqN A)	High precision COS (input in per-unit)	Q=GLOBAL_Q Q=1:30
_iq _IQatan2( _iq A, _iq B) _iqN _IQNatan2( _iqN A, _iqN B)	4-quadrant ATAN (output in radians)	Q=GLOBAL_Q Q=1:29
_iq _IQatan2PU( _iq A, _iq B) _iqN _IQNatanPU( _iqN A, _iqN B)	4-quadrant ATAN (output in per-unit)	Q=GLOBAL_Q Q=1:29
_iq _IQatan( _iq A, _iq B) _iqN _IQNatan( _iqN A, _iqN B)	Arctangent	Q=GLOBAL_Q Q=1:29

**Mathematical Functions:**

Functions	Description	IQ format
_iq _IQexp( _iq A) _iqN _IQNexp( _iqN A)	High precision e raised to the A power	Q=GLOBAL_Q Q=1:29
_iq _IQsqrt( _iq A) _iqN _IQNsqrt( _iqN A)	High precision square root	Q=GLOBAL_Q Q=1:30
_iq _IQisqrt( _iq A) _iqN _IQNisqrt( _iqN A)	High precision inverse square root	Q=GLOBAL_Q Q=1:30
_iq _IQmag( _iq A, _iq B) _iqN _IQNmag( _iqN A, _iqN B)	Magnitude Square: $\sqrt{A^2 + B^2}$	Q=GLOBAL_Q Q=1:30

**Miscellaneous**

Functions	Description	Q format
_iq _IQsat( _iq A, long P, long N)	Saturate the IQ number	Q=GLOBAL_Q
_iq _IQabs( _iq A)	Absolute value of IQ number	Q=GLOBAL_Q

### 5.3. C28x IQmath Library Benchmarks

Function Name	IQ Format	Execution Cycles	Accuracy (in bits)	Program Memory (words)	Input format	Output format	Remarks
<b>Trigonometric Functions</b>							
IQNasin	1-29	154		82 words	IQN	IQN	Note A
IQNsin	1-29	46	30 bits	49 words	IQN	IQN	
IQNsinPU	1-30	40	30 bits	41 words	IQN	IQN	
IQNacos	1-29	170		93 words	IQN	IQN	Note A
IQNcos	1-29	44	30 bits	47 words	IQN	IQN	
IQNcosPU	1-30	38	29 bits	39 words	IQN	IQN	
IQNatan2	1-29	109	26 bits	123 words	IQN	IQN	
IQNatan2PU	1-29	117	27 bits	136 words	IQN	IQN	
IQatan	1-29	109	25 bits	123 words	IQN	IQN	
<b>Mathematical Functions</b>							
IQNexp	1-29	190		61 words	IQN	IQN	Note A
IQNsqrt	1-30	63	29 bits	66 words	IQN	IQN	
IQNisqrt	1-30	64	29 bits	69 words	IQN	IQN	
IQNmag	1-30	86	29 bits	96 words	IQN	IQN	
<b>Arithmetic Functions</b>							
IQNmpy	1-30	~ 6	32 bits	NA	IQN*IQN	IQN	INTRINSIC
IQNrmpy	1-30	17	32 bits	13 words	IQN*IQN	IQN	
IQNrsmPy	1-30	21	32 bits	21 words	IQN*IQN	IQN	
IQNmpyl32	1-30	~ 4	32 bits	NA	IQN*long	IQN	C-MACRO
IQNmpyl32int	1-30	22	32 bits	16 words	IQN*long	long	
IQNmpyl32frac	1-30	24	32 bits	20 words	IQN*long	IQN	
IQNmpyIQX		~ 7	32 bits	NA	IQN*IQN	IQN	INTRINSIC
IQNdiv	1-30	63	28 bits	71 words	IQN/IQN	IQN	
<b>Format Conversion Utilities</b>							
IQN	1-30	NA	N/A	NA	Float	IQN	C-MACRO
IQNtoF	1-30	22	N/A	20 words	IQN	Float	
IQNtoa	1-30	N/A	N/A	210 words	IQN	string	
atolIQN	1-30	N/A	N/A	143 words	char *	IQN	
IQNint	1-30	14	32 bits	8 words	IQN	long	
IQNfrac	1-30	17	32 bits	12 words	IQN	IQN	
IQtoIQN	1-30	~4	N/A	N/A	GLOBAL_Q	IQN	C-MACRO
IQNtoIQ	1-30	~4	N/A	N/A	IQN	GLOBAL_Q	C-MACRO
IQtoQN	1-15	~4	N/A	N/A	GLOBAL_Q	QN	C-MACRO
QNtoIQ	1-15	~4	N/A	N/A	QN	GLOBAL_Q	C-MACRO
<b>Miscellaneous</b>							
IQsat	1-30	~7	N/A	N/A	IQN	IQN	INTRINSIC
IQNabs	1-30	~2	N/A	N/A	IQN	IQN	INTRINSIC



**Notes:**

- A. IQNexp, IQNasin and IQNacos use look-up tables in the IQmathTablesRam section. Refer to Section 3.3.
- B. Execution cycles & Program memory usage mentioned in the Table assumes IQ24 format. Execution cycles may vary by few cycles for some other IQ format. Program memory may vary by few words for some other IQ format.
- C. Execution Cycles mentioned in the table includes the CALL and RETURN (LCR + LRETR) and it assumes that the IQmath table is loaded in internal memory.
- D. Accuracy should always be verified and tested within the end application.

# Chapter 6. Function Descriptions

## 6.1. Conversion Utilities

IQN	Float to IQN data type
-----	------------------------

**Description** This C-macro converts a floating-point constant or variable to the equivalent IQ value.

**Declaration** **Global IQ Macro (IQ format = GLOBAL\_Q)**

```
C      _iq _IQ(float F)
C++    iq  IQ(float F)
```

**Q format specific IQ Macro (IQ format = IQ1 to IQ29)**

```
C      _iqN _IQN(float F)
C++    iq  IQN(float F)
```

**Input** Floating point variable or constant

**Output** **Global IQ Macro (IQ format = GLOBAL\_Q)**  
Fixed point equivalent of floating-point input in GLOBAL\_Q format

**Q format specific IQ Macro (IQ format = IQ1 to IQ29)**  
Fixed point equivalent of floating-point input in IQN format

**Usage** This operation is typically used to convert a floating-point constant or variable to the equivalent IQ value.

**Example 1:** Implement an equation in IQmath

```
// Floating-point equation
Y = M*1.26 + 2.345

// IQmath equation using the GLOBAL_Q value
Y = _IQmpy(M, _IQ(1.26)) + _IQ(2.345)

// IQmath equation specifying the Q value
Y = _IQ23mpy(M, _IQ23(1.26)) + _IQ23(2.345)
```

**Example 2:** Convert a floating-point variable to an IQ data type.

```
#include "IQmathLib.h"
float x=3.343;
_iq y1;
_iq23 y2

y1=_IQ(x)           // Uses the GLOBAL_Q value
y2=_IQ23(x)         // Specifies the Q value
```

**Example 3:** Initialize global variables or tables

```
#include "IQmathLib.h"

// IQmath using GLOBAL_Q
_iq Array[4] =
    {_IQ(1.0), _IQ(2.5) _IQ(-0.2345), _IQ(0.0) }

// IQmath specifying the Q value
_iq23 Array[4] =
    {_IQ23(1.0), _IQ23(2.5) _IQ23(-0.2345), _IQ23(0.0) }
```

**Description** This function converts an IQ number to equivalent floating-point value in IEEE 754 format.

**Declaration** **Global IQ function (IQ format = GLOBAL\_Q)**

```
C      float _IQtoF(_iq A)
C++    float  IQtoF(const iq &A)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      float _IQNtoF(_iqN A)
C++    float  IQNtoF(const iqN &A)
```

**Input** **Global IQ function (IQ format = GLOBAL\_Q)**

Fixed point IQ number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Fixed point IQ number in IQN format.

**Output** Floating point equivalent of fixed-point input.

**Usage** This operation is typically used in cases where the user may wish to perform some operations in floating-point format or convert data back to floating-point for display purposes.

**Example:**

Convert an array of IQ numbers to their equivalent floating-point values

```
_iq DataIQ[N];
float DataF[N];

for(i = 0; i < N; i++)
{
    DataF[i] = _IQtoF(DataIQ[i]);
}
```

<b>Description</b>	This function converts a string to an IQ number.
<b>Declaration</b>	<p><b>Global IQ function (IQ format = GLOBAL_Q)</b></p> <pre>C      float _atoiQ(char *S) C++    float  atoiQ(char *S)</pre> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ30)</b></p> <pre>C      float _atoiQN(char *S) C++    float  atoiQN(char *S)</pre>
<b>Input</b>	<p>This function recognizes (in order) an optional sign, a string of digits optionally containing a radix character.</p> <p>Valid Input strings:            "12.23456", "-12.23456", "0.2345", "0.0", "0", "127", "-89"</p>
<b>Output</b>	<p>The first unrecognized character ends the string and returns zero. If the input string converts to a number greater then the max/min values for the given Q value, then the returned value will be limited to the min/max values</p> <p><b>Global IQ function (IQ format = GLOBAL_Q)</b>            Fixed point equivalent of input string in GLOBAL_Q format</p> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ29)</b>            Fixed point equivalent of input string in IQN format</p>
<b>Usage</b>	<p>This is useful for programs that need to process user input or ASCII strings.</p> <p><b>Example:</b></p> <p>The following code prompts the user to enter the value X:</p> <pre>char buffer[N]; _iq X;  printf("Enter value X = "); gets(buffer); X = _atoiQ(buffer);           // IQ value (GLOBAL_Q)</pre>

**Description** This function converts an IQ number to a string.

**Declaration Global IQ function (IQ format = GLOBAL\_Q)**

```
C      int _IQtoa(char *string, const char *format, _iq x)
C++    int  IQtoa(char *string, const char *format,
              const iq &x)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      int _IQNtoa(char *string, const char *format, _iqN x)
C++    int  IQNtoa(char *string, const char *format,
              const iqN &x)
```

**Input** string: output string

format: conversion format. Must be of the form "%xx.yyf" with xx and yy at most 2 characters in length.  
For Example: "%10.12f", "%2.4f", "%11.6f"  
The maximum supported integer field width (xx) is 11 (including any negative sign). This captures the full integer range for I2Q30 to I31Q1 numbers.

x: Global IQ function: input value in IQ format  
Q format specific function: input value in IQN format

**Output** The output string is returned in the location pointed to by the "string" argument.

If you are using MATH\_TYPE set to IQ\_MATH, then the return integer value is an error code with the following possible values:

- 0 = no error
- 1 = width too small to hold integer characters
- 2 = illegal format specified

If you are using MATH\_TYPE set to FLOAT\_MATH, then sprintf() is called and the return integer value is the number of characters written.

**Usage**

- Any leading zeros are not printed for the integer part. Hence, the format specifies the maximum width of the integer field. The field may be smaller.
- The output string is terminated with the null character.
- The integer width in "format" includes the negative sign for negative numbers, e.g. -12.3456 is "%3.5f"
- The decimal width in "format" includes the decimal point. For example: -12.3456 is "%3.5f"
- "string" must be large enough to hold the output (including the negative sign, and the terminating null character). The program does not check for overrun. Memory corruption will occur if "string" is too small.
- A non-zero return value indicates that the output string is invalid.

**Example:**

```
char buffer[30];

_iq   x1 = _IQ(1.125);
_iq1  x2 = _IQ1(-6789546.3);
_iq14 x3 = _IQ14(-432.6778);
_iq30 x4 = _IQ30(1.127860L);
int error;

// Global_Q
error = _IQtoa(buffer, "%10.10f", x1);

// IQ1
error = _IQ1toa(buffer, "%8.2f", x2);

// IQ14
error = _IQ14toa(buffer, "%6.6f", x3);

// IQ30
error = _IQ30toa(buffer, "%11.12f", x4);
```

**Description** This function returns the integer portion of IQ number.

**Declaration Global IQ function (IQ format = GLOBAL\_Q)**

```
C      long _IQint(_iq A)
C++    long  IQint(const iq &A)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      long _IQNint(_iqN A)
C++    long  IQNint(const iqN &A)
```

**Input Global IQ function (IQ format = GLOBAL\_Q)**

Fixed point IQ number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Fixed point IQ number in IQN format.

**Output** Integer part of the IQ number

**Usage Example 1:**

Extract the integer and fractional part of an IQ number.

```
_iq Y0 = 2.3456;
_iq Y1 = -2.3456
long Y0int, Y1int;
_iq Y0frac, Y1frac;

Y0int  = _IQint(Y0);    // Y0int = 2
Y1int  = _IQint(Y1);    // Y1int = -2
Y0frac = _IQfrac(Y0);   // Y0frac = 0.3456
Y1frac = _IQfrac(Y1);   // Y1frac = -0.3456
```

**Example 2:**

Build an IQ number from an integer and fractional part

```
_iq Y;
long Yint;
_iq Yfrac;

Y = _IQmpyI32(_IQ(1.0), Yint) + Yfrac;
```



**Description** This function returns the fractional portion of IQ number.

**Declaration Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQfrac(_iq A)
C++    iq  IQfrac(const iq &A)
```

**Q format specific IQ function (IQ format = N = 1 to 30)**

```
C      _iqN _IQNfrac(_iqN A)
C++    iqN IQNfrac(const iqN &A)
```

**Input Global IQ function (IQ format = GLOBAL\_Q)**

Fixed point IQ number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Fixed point IQ number in IQN format.

**Output** Fractional part of the IQ number

**Usage Example 1:**

Extract the integer and fractional part of an IQ number

```
_iq Y0 = _IQ(2.3456);
_iq Y1 = _IQ(-2.3456);
long Y0int, Y1int;
_iq Y0frac, Y1frac;

Y0int = _IQint(Y0);    // Y0int = 2
Y1int = _IQint(Y1);    // Y1int = -2
Y0frac = _IQfrac(Y0);  // Y0frac = 0.3456
Y1frac = _IQfrac(Y1);  // Y1frac = -0.3456
```

**Example 2:**

Build an IQ number from an integer and fractional part.

```
_iq Y;
long Yint;
_iq Yfrac;

Y = _IQmpyI32(_IQ(1.0), Yint) + Yfrac;
```

**Description** This Macro converts an IQ number in GLOBAL\_Q format to the specified IQ format.

**Declaration** C `_iqN _IQtoIQN(_iq A)`  
C++ `iqN IQtoIQN(const iq &A)`

**Input** IQ number in GLOBAL\_Q format

**Output** Equivalent value of input in IQN format

**Usage** This macro may be used in cases where a calculation may temporarily overflow the IQ value resolution and hence require a different IQ value to be used for the intermediate operations.

**Example:**

The Following example calculates the magnitude of complex number (X+jY) in Q26 format:

```
Z = sqrt(X^2 + Y^2)
```

The values Z, X, Y are given as GLOBAL\_Q = 26, but the equation itself may generate an overflow.

To guard against this, the intermediate calculations will be performed using Q = 23 and the value converted back at the end as shown below:

```
#include "IQmathLib.h"
_iq Z, Y, X;           // GLOBAL_Q = 26
_iq23 temp;

temp = _IQ23sqrt( _IQ23mpy(_IQtoIQ23(X), _IQtoIQ23(X)) +
                 _IQ23mpy(_IQtoIQ23(Y), _IQtoIQ23(Y)) );

Y = _IQ23toIQ(temp);
```

**Description** This Macro converts an IQ number in IQN format to the GLOBAL\_Q format.

**Declaration** C `_iq _IQNtoIQ(_iqN A)`  
 C++ `iq IQNtoIQ(const iqN &A)`

**Input** IQ number in IQN format

**Output** Equivalent value of input in GLOBAL\_Q format

**Usage** This macro may be used in cases where the result of the calculation performed in different IQ resolution to be converted to GLOBAL\_Q format.

**Example:**

Following example calculates the magnitude of complex number (X+jY) in Q26 format:

```
Z = sqrt(X^2 + Y^2)
```

The values Z, X, Y are given as GLOBAL\_Q = 26, but the equation itself may generate an overflow. To guard against this, the intermediate calculations will be performed using Q = 23 and the value converted back at the end as shown below:

```
#include "IQmathLib.h"
_iq Z, Y, X;           // GLOBAL_Q = 26
_iq23 temp;

temp = _IQ23sqrt( _IQ23mpy(_IQtoIQ23(X), _IQtoIQ23(X)) +
                 _IQ23mpy(_IQtoIQ23(Y), _IQtoIQ23(Y)) );

Y = _IQ23toIQ(temp);
```

**Description** This Macro converts a 32-bit number in GLOBAL\_Q format to 16-bit number in QN format.

**Declaration**

```
C      int _IQtoQN(_iq A)
C++    int  IQtoQN(const iq &A)
```

**Input** IQ number in GLOBAL\_Q format

**Output** Equivalent value of input in QN format (16-bit fixed point number)

**Usage** This macro may be used in cases where the input and output data is 16-bits, but the intermediate operations are operated using IQ data types.

**Example:**

Sum of product computation using the input sequence that is not in GLOBAL\_Q format:

```
Y = X0*C0 + X1*C1 + X2*C2 // X0, X1, X2 in Q15 format
                          //C0,C1, C2 in GLOBAL_Q format
```

We can convert the Q15 values to IQ, perform the intermediate sums using IQ and then store the result back as Q15:

```
short X0, X1, X2;           // Q15 short
iq  C0, C1, C2;            // GLOBAL_Q
short Y;                   // Q15
_iq sum                    // IQ (GLOBAL_Q)

sum = _IQmpy(_Q15toIQ(X0), C0);
sum += _IQmpy(_Q15toIQ(X1), C1);
sum += _IQmpy(_Q15toIQ(X2), C2);
Y = _IQtoQ15(sum);
```

**Description** This Macro converts a 16-bit number in QN format to 32-bit number in GLOBAL\_Q format.

**Declaration** C `_iq _QNtoIQ(int A)`  
C++ `iq QNtoIQ(int A)`

**Input** 16-bit fixed point number in QN format

**Output** Equivalent value of input in GLOBAL\_Q format

**Usage** This macro may be used in cases where the input and output data is 16-bits, but the intermediate operations are operated using IQ data types.

**Example:**

Sum of product computation using the input sequence that is not in GLOBAL\_Q format:

```
Y = X0*C0 + X1*C1 + X2*C2 // X0, X1, X2 in Q15 format
                          // C0, C1, C2 in GLOBAL_Q format
```

We can convert the Q15 values to IQ, perform the intermediate sums using IQ and then store the result back as Q15:

```
short X0, X1, X2;           // Q15 short
iq C0, C1, C2;             // GLOBAL_Q
short Y;                   // Q15
_iq sum                    // IQ (GLOBAL_Q)

sum = _IQmpy(_Q15toIQ(X0), C0);
sum += _IQmpy(_Q15toIQ(X1), C1);
sum += _IQmpy(_Q15toIQ(X2), C2);
Y = _IQtoQ15(sum);
```

## 6.2. Arithmetic Operations

IQNmpy	<i><b>IQ Multiplication (IQN*IQN)</b></i>
--------	---

**Description** This C compiler intrinsic multiplies two IQ number. It does not perform saturation and rounding. In most cases, the multiplication of two IQ variables will not exceed the range of the IQ variable. This operation takes the least amount of cycles and code size and should be used most often.

**Declaration** **Global IQ intrinsic (IQ format = GLOBAL\_Q)**

```
C      __iq __IQmpy(__iq A, __iq B)
C++    iq operator * (const iq &A, const iq &B)
        iq &iq :: operator *= (const iq &A)
```

**Q format specific IQ intrinsic (IQ format = IQ1 to IQ30)**

```
C      __iqN __IQNmpy(__iqN A, __iqN B)
C++    iqN operator * (const iqN &A, const iqN &B)
        iqN &iqN :: operator *= (const iqN &A)
```

**Input** **Global IQ intrinsic (IQ format = GLOBAL\_Q)**  
Inputs A and B are IQ numbers in GLOBAL\_Q format

**Q format specific IQ intrinsic (IQ format = IQ1 to IQ30)**  
Inputs A and B are IQ numbers in IQN format

**Output** **Global IQ intrinsic (IQ format = GLOBAL\_Q)**  
Result of multiplication in GLOBAL\_Q format

**Q format specific IQ intrinsic (IQ format = IQ1 to IQ30)**  
Result of multiplication in IQN format.

**Usage** **Example 1;**

Compute  $Y = M * X + B$  in GLOBAL\_Q format with no rounding or saturation.

```
__iq Y, M, X, B;
Y = __IQmpy(M, X) + B;
```

**Example 2:**

Compute  $Y = M * X + B$  in IQ10 format with no rounding or saturation, assuming M, X, B are represented in IQ10 format.

```
__iq10 Y, M, X, B;
Y = __IQ10mpy(M, X) + B;
```

**Description** This function multiplies two IQ number and rounds the result. In cases where absolute accuracy is necessary, this operation performs the IQ multiply and rounds the result before storing back as an IQ number. This gives an additional 1/2 LSBit of accuracy.

**Declaration Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQrmpy(_iq A, _iq B)
C++    iq  IQrmpy(const iq &A, const iq &B)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      _iqN _IQNrmpy(_iqN A, _iqN B)
C++    iqN  IQNrmpy(const iqN &A, const iqN &B)
```

**Input Global IQ function (IQ format = GLOBAL\_Q)**

Input "A" & "B" are IQ number in GLOBAL\_Q format

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Input "A" & "B" are IQ number in IQN format

**Output Global IQ function (IQ format = GLOBAL\_Q)**

Result of multiplication in GLOBAL\_Q format

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Result of multiplication in IQN format.

**Usage Example 1:**

Compute  $Y = M * X + B$  in GLOBAL\_Q format with rounding but without saturation.

```
_iq Y, M, X, B;
Y = _IQrmpy(M, X) + B;
```

**Example 2:**

Compute  $Y = M * X + B$  in IQ10 format with rounding but without saturation.

```
_iq10 Y, M, X, B;
Y = _IQ10rmpy(M, X) + B;
```

**Description** This function multiplies two IQ number with rounding and saturation. In cases where the calculation may possibly exceed the range of the IQ variable, then this operation will round and then saturate the result to the maximum IQ value range before storing.

**Declaration Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQrsmPy(_iq A, _iq B)
```

```
C++   iq  IQrsmPy(iq &A, iq &B)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      _iqN _IQNrsmPy(_iqN A, _iqN B)
```

```
C++   iqN  IQNrsmPy(const iqN &A, const iqN &B)
```

**Input Global IQ function (IQ format = GLOBAL\_Q)**

Input "A" & "B" are IQ number in GLOBAL\_Q format

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Input "A" & "B" are IQ number in IQN format

**Output Global IQ function (IQ format = GLOBAL\_Q)**

Result of multiplication in GLOBAL\_Q format

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Result of multiplication in IQN format.

**Usage** Let us assume that we use IQ26 are GLOBAL\_Q format. This means that the range of the numbers is approximately [-32.0, 32.0] (Refer section 3.2). If two IQ variables are multiplied together, then the maximum range of the result is [-1024, 1024]. This operation would make sure that the result is saturated to +/- 32 in cases where the result exceeds this.

**Example 1:**

Compute  $Y = M \times X$  in the GLOBAL\_Q format with rounding and saturation. Assume GLOBAL\_Q=IQ26 in the IQmath header file.

```
_iq Y, M, X;
```

```
M=_IQ(10.9);          // M=10.9
```

```
X=_IQ(4.5);           // X=4.5
```

```
Y = _IQrmpy(M,X);     // Y= ~32.0, output is Saturated to MAX
```

**Example 2:**

Compute  $Y = M \times X$  in IQ26 format with rounding and saturation.

```
_iq26 Y, M, X;
```

```
M=_IQ26(-10.9);       // M=-10.9
```

```
X=_IQ26(4.5);         // X=4.5
```

```
Y = _IQ26rmpy(M,X);   // Y= -32.0, saturated to MIN
```



**Description** This macro multiplies an IQ number with a long integer.

**Declaration Global IQ Macro (IQ format = GLOBAL\_Q)**

```
C      _iq _IQmpyI32(_iq A, long B)
C++    iq  IQmpyI32(const iq &A, long B)
```

**Q format specific IQ Macro (IQ format = IQ1 to IQ30)**

```
C      _iqN _IQNmpyI32(_iqN A, long B)
C++    iqN  IQNmpyI32(const iqN &A, long B)
```

**Input Global IQ Macro (IQ format = GLOBAL\_Q)**

Operand A is an IQ number in GLOBAL\_Q format and B is the long integer.

**Q format specific IQ Macro (IQ format = IQ1 to IQ30)**

Operand A is an IQ number in IQN format and B is the long integer.

**Output Global IQ Macro (IQ format = GLOBAL\_Q)**

Result of multiplication in GLOBAL\_Q format

**Q format specific IQ Macro (IQ format = IQ1 to IQ30)**

Result of multiplication in IQN format.

**Usage Example 1:**

Compute  $Y = 5 \times X$  in the GLOBAL\_Q format. Assume GLOBAL\_Q = IQ26 in the IQmath header file.

```
_iq Y, X;

X = _IQ(5.1);           // X=5.1 in GLOBAL_Q format
Y = IQmpyI32(X, 5);     // Y= 25.5 in GLOBAL_Q format
```

**Example 2:**

Compute  $Y = 5 \times X$  in IQ26 format.

```
_iq26 Y, X;
long M;

M=5;           // M=5
X = _IQ26(5.1); // X=5.1 in IQ29 format
Y = _IQ26mpyI32(X, M); // Y=25.5 in IQ29 format
```

**Description** This function multiplies an IQ number with a long integer and returns the integer part of the result.

**Declaration Global IQ function (IQ format = GLOBAL\_Q)**

```
C      long _IQmpyI32int(_iq A, long B)
C++    long IQmpyI32int(const iq &A, long B)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      long _IQNmpyI32int(_iqN A, long B)
C++    long IQNmpyI32int(const iqN &A, long B)
```

**Input Global IQ function (IQ format = GLOBAL\_Q)**

Operand "A" is an IQ number in GLOBAL\_Q format and "B" is the long integer.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Operand "A" is an IQ number in IQN format and "B" is the long integer.

**Output Global IQ function (IQ format = GLOBAL\_Q)**

Integer part of the result (32-bit)

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Integer part of the result (32-bit)

**Usage Example 1**

Convert an IQ value in the range [- 1.0, +1.0] to a DAC value with the range [ 0 to 1023]:

```
_iq Output;
long temp;
short OutputDAC;

// value converted to +/- 512
temp = _IQmpyI32int(Output, 512);
// value scaled to 0 to 1023
temp += 512;
// saturate within range of DAC
if( temp > 1023 )temp = 1023;
if( temp < 0 ) temp = 0;
// output to DAC value
OutputDAC = (int )temp;
```

**Note:** The integer operation performs the multiply and calculates the integer portion from the resulting 64-bit calculation. Hence it avoids any overflow conditions.

**Description** This function multiplies an IQ number with a long integer and returns the fractional part of the result.

**Declaration Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQmpyI32frac(_iq A, long B)
C++    iq  IQmpyI32frac(const iq &y, long x)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      _iqN _IQNmpyI32frac(_iqN A, long B)
C++    iqN  IQNmpyI32frac(const iqN &A, long B)
```

**Input Global IQ function (IQ format = GLOBAL\_Q)**

Operand A is an IQ number in GLOBAL\_Q format and B is a long integer.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Operand A is an IQ number in IQN format and B is the long integer.

**Output Global IQ function (IQ format = GLOBAL\_Q)**

Fractional part of the result (32-bit)

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Fractional part of the result (32-bit)

**Usage**

**Example:**

The following example extracts the fractional part of result after multiplication (Assuming GLOBAL\_Q=IQ26)

```
_iq  X1= _IQ(2.5);
_iq  X2= _IQ26(-1.1);
_iq  Y1frac, Y2frac;
long M1=5, M2=9;

// Y1frac = 0.5 in GLOBAL_Q
Y1frac = IQmpyI32frac(X1, M1);
// Y2frac = -0.9 in GLOBAL_Q
Y2frac = IQ26mpyI32frac(X2, M2);
```

**Description** This C compiler intrinsic multiplies two IQ number that are represented in different IQ format

**Declaration Global IQ Intrinsic (IQ format = GLOBAL\_Q)**

```
C      _iq _IQmpyIQX(_iqN1 A, int N1, _iqN2 B, int N2)
C++    iq  IQmpyIQX(iqN1 A, int N1, iqN2 B, int N2)
```

**Q format specific IQ Intrinsic (IQ format = IQ1 to IQ30)**

```
C      _iqN _IQNmpyIQX(_iqN1 A, int N1, _iqN2 B, int N2)
C++    iqN  IQNmpyIQX(iqN1 A, int N1, iqN2 B, int N2)
```

**Input** Operand “A” is an IQ number in “IQN1” format and operand “B” is in “IQN2” format.

**Output** **Global IQ Intrinsic (IQ format = GLOBAL\_Q)**  
Result of the multiplication in GLOBAL\_Q format

**Q format specific IQ Intrinsic (IQ format = IQ1 to IQ30)**

Result of the multiplication in IQN format

**Usage** This operation is useful when we wish to multiply values of different IQ.

**Example:**

Calculate the following equation:  $Y = X0 * C0 + X1 * C1 + X2 * C2$

Where,

X0, X1, X2 values are in IQ30 format (Range -2 to +2)

C0, C1, C2 values are in IQ28 format (Range -8 to +8)

The maximum range of Y will be -48 to +48. Therefore, we will store the result in an IQ format that is less than IQ25.

**Case 1: GLOBAL\_Q=IQ25**

```
_iq30 X0, X1, X2;          // All values IQ30
_iq28 C0, C1, C2;          // All values IQ28
_iq Y;                      // Result GLOBAL_Q = IQ25
```

```
Y = _IQmpyIQX(X0, 30, C0, 28);
Y += _IQmpyIQX(X1, 30, C1, 28);
Y += _IQmpyIQX(X2, 30, C2, 28);
```

**Case 2: IQ Specific computation**

```
_iq30 X0, X1, X2;          // All values IQ30
_iq28 C0, C1, C2;          // All values IQ28
_iq25 Y;                    // Result GLOBAL_Q = IQ25
```

```
Y = _IQ25mpyIQX(X0, 30, C0, 28);
Y += _IQ25mpyIQX(X1, 30, C1, 28);
Y += _IQ25mpyIQX(X2, 30, C2, 28);
```

**Description** This module divides two IQN number and provide 32-bit quotient (IQN format) using Newton-Raphson technique

**Declaration** **Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQdiv(_iq A, _iq B)
C++    iq operator / (const iq &A, const iq &B)
        iq &iq :: operator /= (const iq &A)

Q format specific IQ function (IQ format = IQ1 to IQ30)
C      _iqN _IQNdiv(_iqN A, iq B)
C++    iqN operator / (const iqN &A, const iqN &B)
        iqN &iqN :: operator /= (const iqN &A)
```

**Input** **Global IQ function (IQ format = GLOBAL\_Q)**  
Input "A" & "B" are fixed-point number represented in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**  
Input 'A' & 'B' are fixed-point number in IQN format (N=1:30)

**Output** **Global IQ function (IQ format = GLOBAL\_Q)**  
Output in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**  
Output in IQN format (N=1:30)

**Accuracy**  $= 20\log_2(2^{31}) - 20\log_2(7) = 28$  bits

**Usage** **Example:**

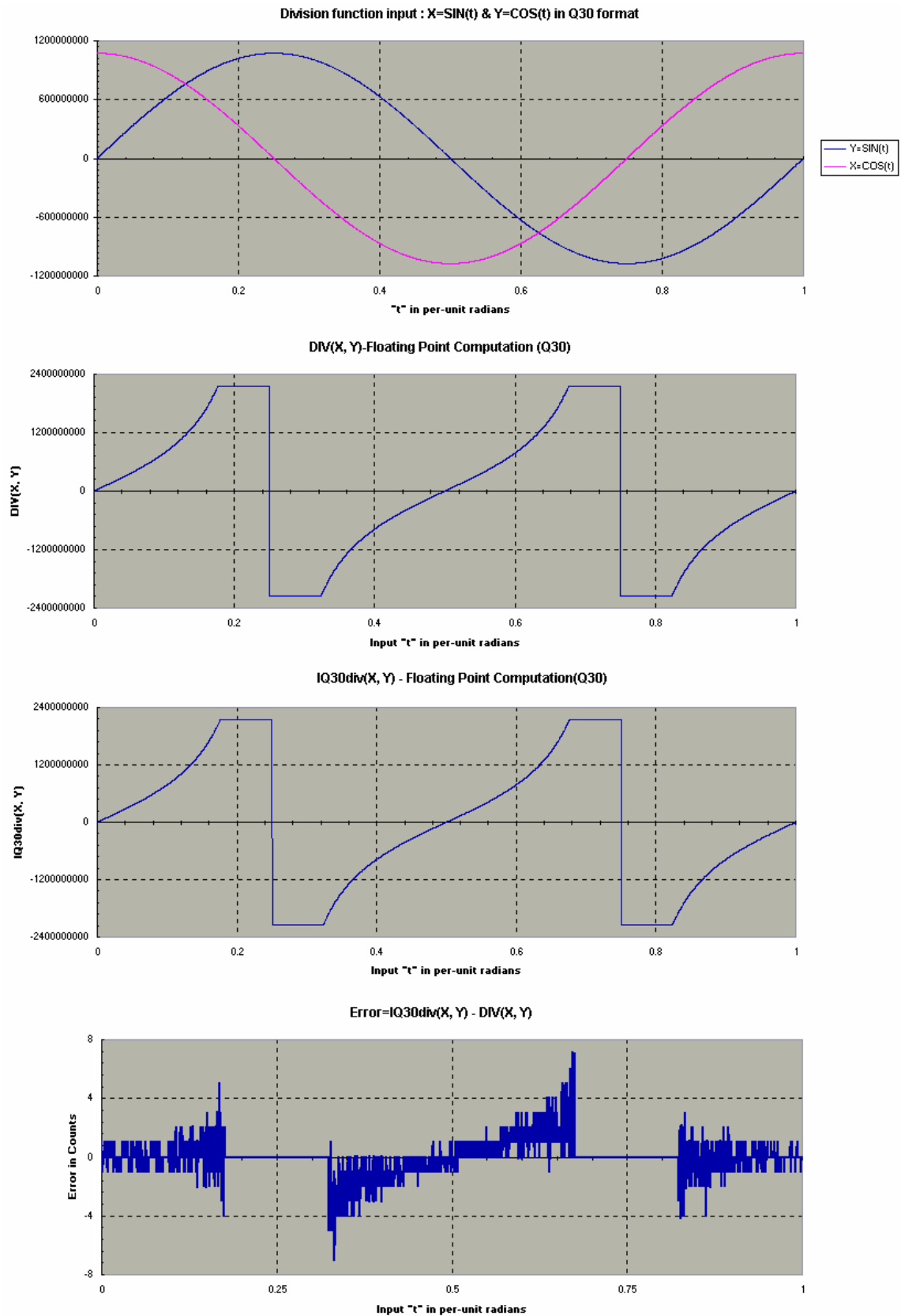
The following example obtains  $\frac{1}{5} = 0.666$  assuming that GLOBAL\_Q is set to Q28 format in the IQmath header file.

```
#include "IQmathLib.h"
_iq in1 out1;
_iq28 in2 out2;

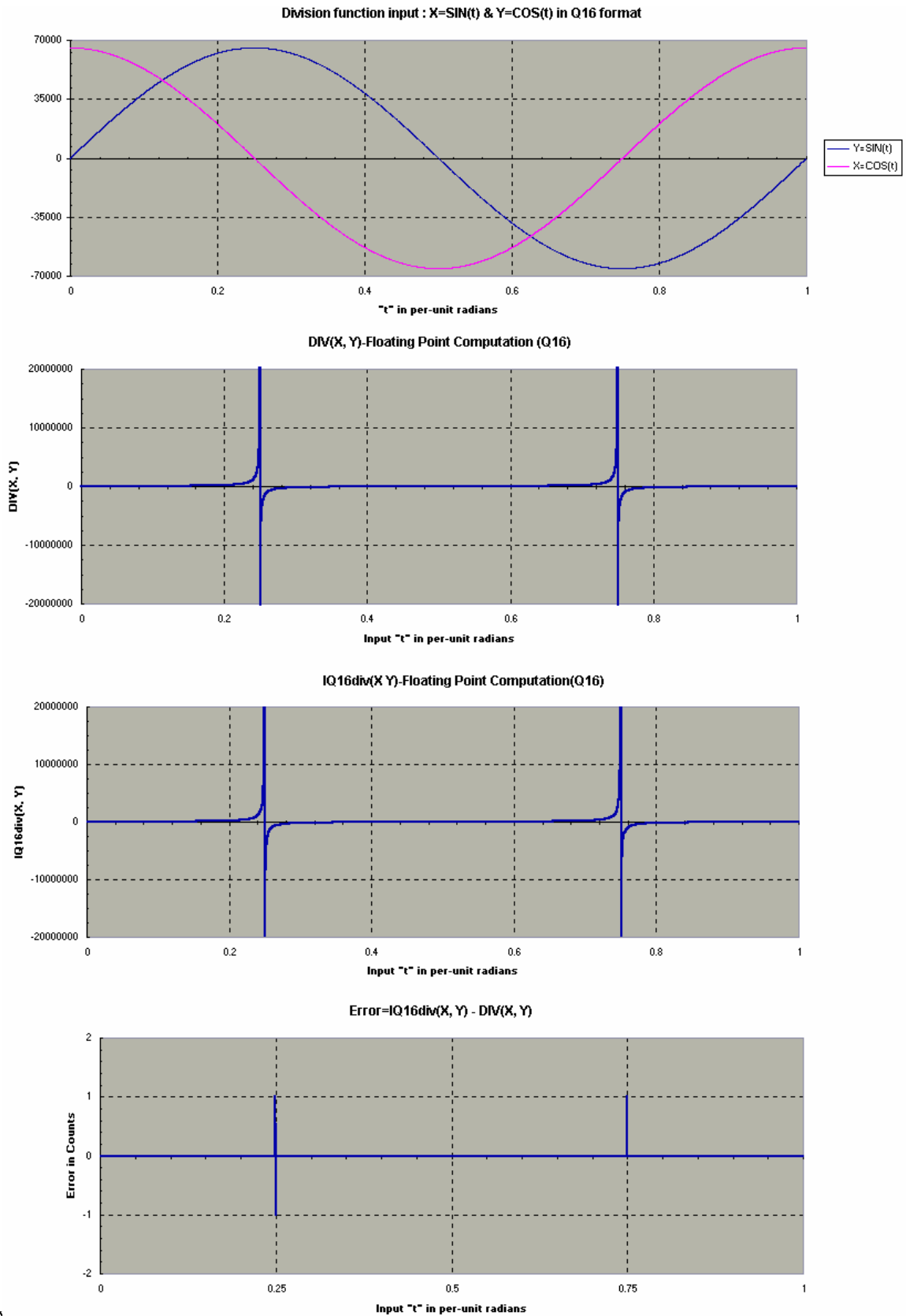
void main(void )
{
    in1  = _IQ(1.5);
    out1 = _IQdiv(_IQ(1.0), in1);

    in2  = _IQ28(1.5);
    out2 = _IQ28div(_IQ28(1.0), in2);
}
```

## Fixed Point division vs. C Float division



## Fixed Point division vs. C Float division



### 6.3. Trigonometric Functions

IQNasin	<i>Fixed point ASIN (radians)</i>
<b>Description</b>	This module computes the inverse sine of the input and returns the result in radians.
<b>Declaration</b>	<p><b>Global IQ function (IQ format = GLOBAL_Q)</b></p> <pre>C      _iq _IQasin(_iq A) C++    iq  IQasin(const iq &amp;A)</pre> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ29)</b></p> <pre>C      _iqN _IQNasin(_iqN A) C++    iqN IQNasin(const iqN &amp;A)</pre>
<b>Input</b>	<p><b>Global IQ function (IQ format = GLOBAL_Q)</b> Input argument is in radians and represented as fixed-point number in GLOBAL_Q format.</p> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ29)</b> Input argument is in radians and represented as fixed-point number in IQN format (N=1:29).</p>
<b>Output</b>	<p><b>Global IQ function (IQ format = GLOBAL_Q)</b> This function returns the inverse sine of the input argument as fixed-point number in GLOBAL_Q format.</p> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ29)</b> This function returns the inverse sine of the input argument as fixed-point number in IQN format (N=1:29)</p>
<b>Example</b>	<p>The following example obtains the result of the equation <math>\text{asin}(0.70710678) = (.25 \times \pi)</math>. It assumes that GLOBAL_Q is set to Q29 format in the IQmath header file.</p>

```
#include "IQmathLib.h"
#define PI 3.14156
_iq in1, out1;
_iq29 in2, out2;

void main(void )
{
// in1 = in2 = 0.70710678L x 2^29 = 0x16A09E60
// out1 = out2 = asin(0.70710678) = 0x1921FB4A

    in1 = _IQ(0.70710678L);
    out1 = _IQasin(in1);

    in2 = _IQ29(0.70710678L)
    out2 = _IQ29asin(in2);
}
```



**Description** This module computes the sine value of the input (in radians) using table look-up and Taylor series expansion between the look-up table entries.

**Declaration** **Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQsin(_iq A)
C++    iq  IQsin(const iq &A)
```

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

```
C      _iqN _IQNsin(_iqN A)
C++    iqN IQNsin(const iqN &A)
```

**Input** **Global IQ function (IQ format = GLOBAL\_Q)**

Input argument is in radians and represented as fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

Input argument is in radians and represented as fixed-point number in IQN format (N=1:29).

**Output** **Global IQ function (IQ format = GLOBAL\_Q)**

This function returns the sine of the input argument as fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

This function returns the sine of the input argument as fixed-point number in IQN format (N=1:29)

**Accuracy**  $= 20\log_2(\pi \times 2^{29}) - 20\log_2(1) = 30$  bits

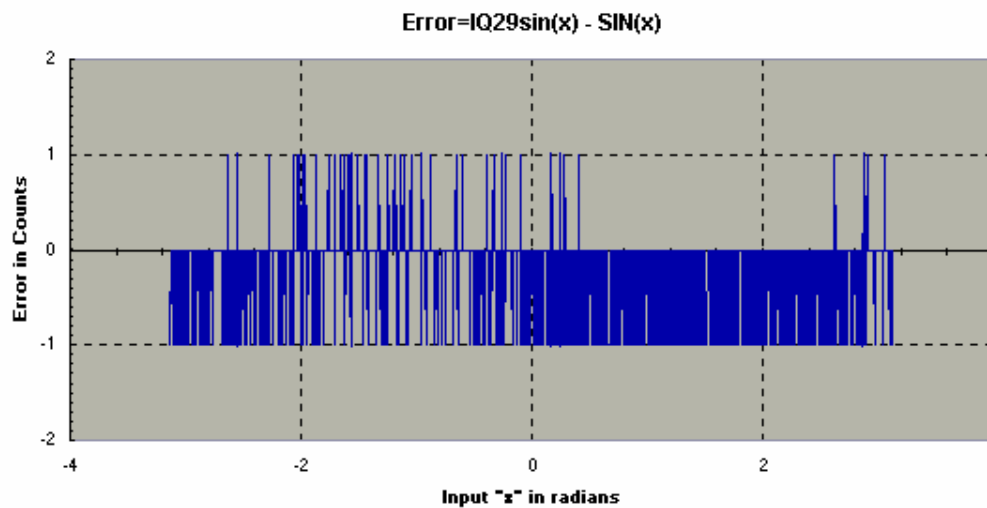
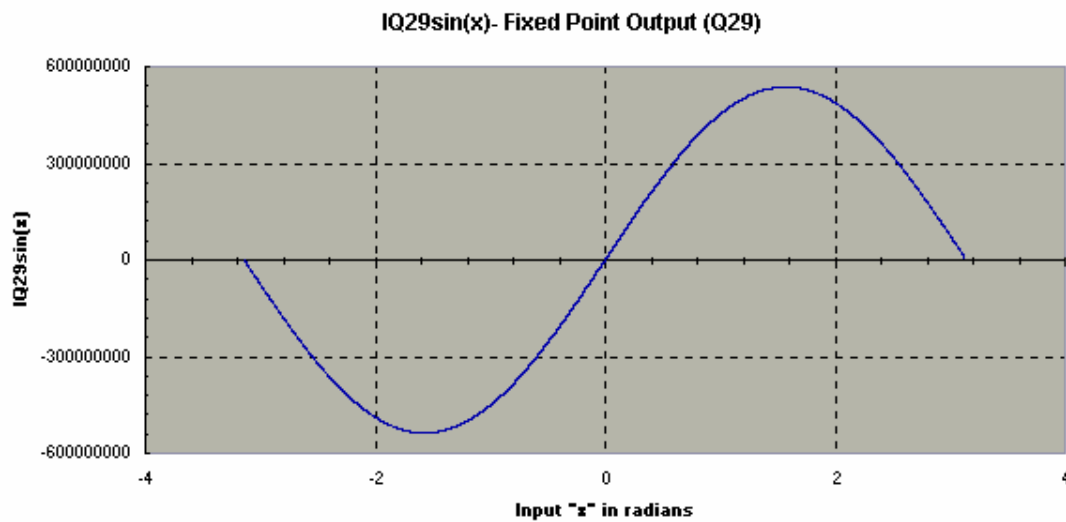
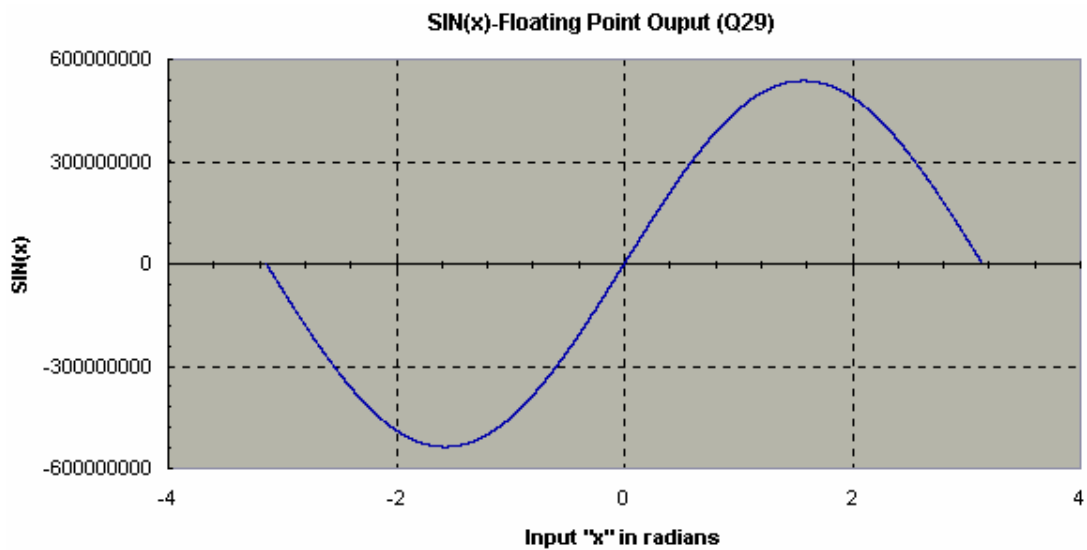
**Example** The following example obtains  $\sin(0.25 \times \pi) = 0.707$  assuming that GLOBAL\_Q is set to Q29 format in the IQmath header file.

```
#include "IQmathLib.h"
#define PI 3.14156
_iq in1, out1;
_iq28 in2, out2;

void main(void ){
// in1 = 0.25 x pi x 2^29 = 0x1921FB54
// out1 = sin(0.25 x pi)x 2^29 = 0x16A09E66
// in2 = 0x25 x pi x 2^29 = 0x1921FB54
// out2 = sin(0.25 x pi)x 2^29 = 0x16A09E66

    in1=_IQ(0.25*PI);
    out1=_IQsin(in1)
    in2=_IQ29(0.25*PI)
    out2=_IQ29sin(in2);
}
```

**IQNsin Function vs. C Float SIN:** Input varies from  $-\pi$  to  $\pi$



**Description** This module computes the sine value of the input (in per-unit radians) using table look-up and Taylor series expansion between the look-up table entries.

**Declaration** **Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQsinPU(_iq A)
C++    iq  IQsinPU(const iq &A)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      _iqN _IQNsinPU(_iqN A)
C      iqN  IQNsinPU(const iqN &A)
```

**Input** **Global IQ function (IQ format = GLOBAL\_Q)**

Input argument is in per-unit radians and represented as fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Input argument is in per-unit radians and represented as fixed-point number in IQN format (N=1:30).

**Output** **Global IQ function (IQ format = GLOBAL\_Q)**

This function returns the sine of the input argument as fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

This function returns the sine of the input argument as fixed-point number in IQN format (N=1:30)

**Accuracy**  $= 20\log_2(1 \times 2^{30}) - 20\log_2(1) = 30$  bits

**Usage** **Example:**

The following example obtains the  $\sin(0.25 \times \pi) = 0.707$  assuming that GLOBAL\_Q is set to Q30 format in the IQmath header file.

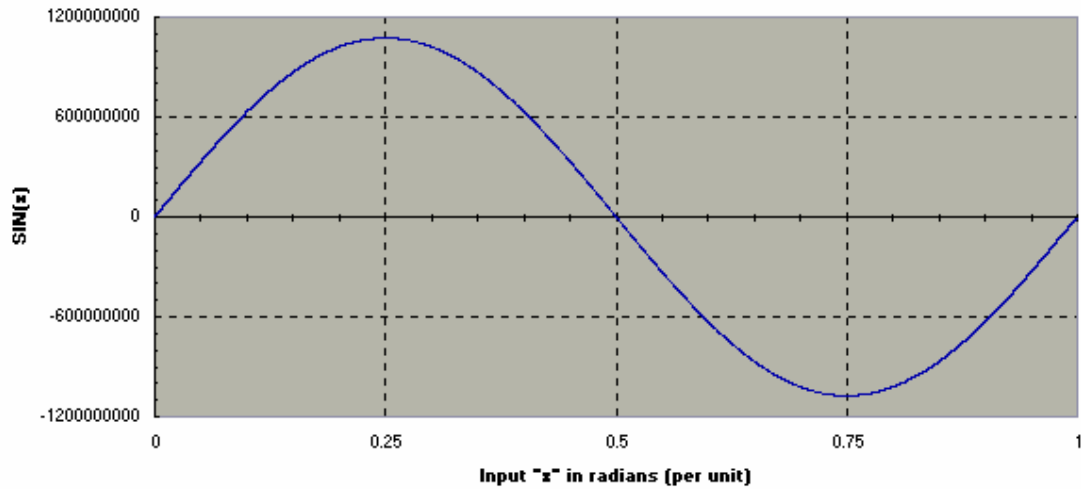
```
#include "IQmathLib.h"
#define PI 3.14156
_iq in1, out1;
_iq30 in2, out2;

void main(void ){
// in1  = (0.25 x PI)/(2PI) x 2^30 = 0x08000000
// out1 = sin(0.25 x PI)x 2^30 = 0x2D413CCC
// in2  = (0.25 x PI)/(2PI) x 2^30 = 0x08000000
// out2 = sin(0.25 x PI)x 2^30 = 0x2D413CCC

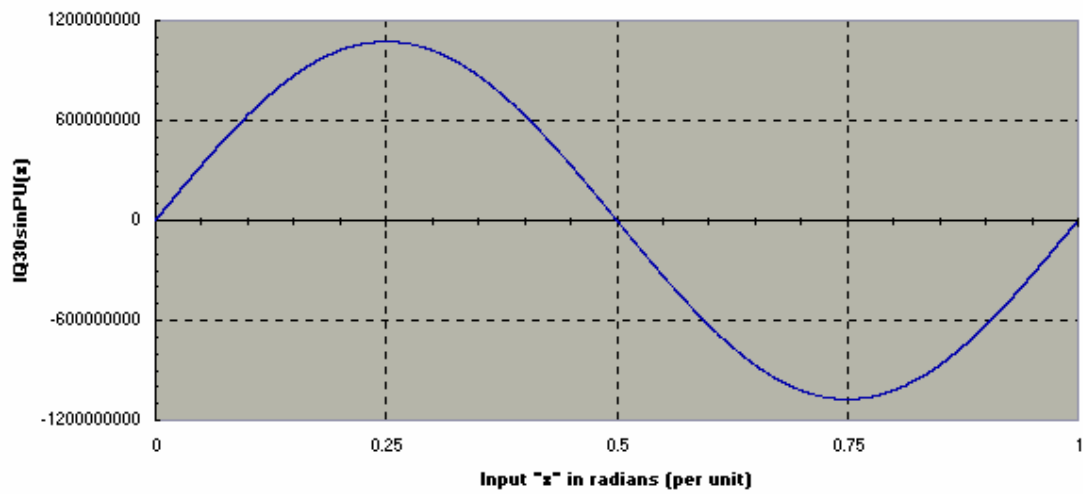
    in1  = _IQ(0.25L*PI);
    out1 = _IQsinPU(in1)
    in2  = _IQ30(0.25*PI/PI);
    out2 = _IQ30sinPU(in2);
}
```

**IQNsinPU Function vs. C Float SIN:** Input varies from 0 to  $2\pi$  in per unit representation

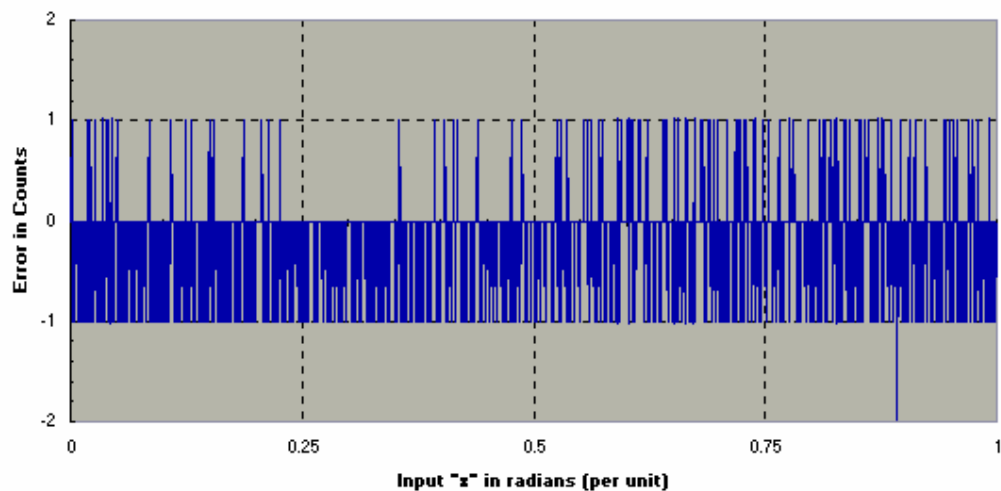
**SIN(x)-Floating Point Output (Q30)**



**IQ30sinPU(x)- Fixed Point Output (Q30)**



**Error=IQ30sinPU(x) - SIN(x)**



**Description** This module computes the inverse cosine of the input and returns the result in radians.

**Declaration Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQacos(_iq A)
C++    iq  IQacos( const iq & A)
```

**Q format specific IQ function (IQ format = N = 1 to 29)**

```
C      _iqN _IQNacos(_iqN A)
C++    iq N  IQNacos(const iqN &A)
```

**Input Global IQ function (IQ format = GLOBAL\_Q)**

Input argument is in radians and represented as fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

Input argument is in radians and represented as fixed-point number in IQN format (N=1:29).

**Output Global IQ function (IQ format = GLOBAL\_Q)**

This function returns the inverse cosine of the input argument as fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

This function returns the inverse cosine of the input argument as fixed-point number in IQN format (N=1:29)

**Example** The following example obtains the result of  $\text{asin}(0.70710678) = (0.25 \times \pi)$  assuming that GLOBAL\_Q is set to Q29 format in the IQmath header file.

```
#include "IQmathLib.h"
_iq in1, out1;
_iq29 in2, out2;

void main(void )
{
// in1  = 0x70710678 x 2^29 = 0x16A09E60
// out1 = acos(0.70710678L) x 2^29 = 0x1921FB5E
// in2  = 0x70710678 x 2^29 = 0x16A09E60
// out2 = acos(0.70710678L) x 2^29 = 0x1921FB5E

    in1  = _IQ(0.70710678L);
    out1 = _IQacos(in1);
    in2  = _IQ29(0.70710678L)
    out2 = _IQ29acos(in2);

}
```

**Description** This module computes the cosine value of the input (in radians) using table look-up and Taylor series expansion between the look up table entries.

**Declaration** **Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQcos(_iq A)
C++    iq  IQcos(const iq &A)
```

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

```
C      _iqN _IQNcos(_iqN A)
C++    iqN IQNcos(const iqN &A)
```

**Input** **Global IQ function (IQ format = GLOBAL\_Q)**

Input argument is in radians and represented as fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

Input argument is in radians and represented as fixed-point number in IQN format (N=1:29).

**Output** **Global IQ function (IQ format = GLOBAL\_Q)**

This function returns the cosine of the input argument as fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

This function returns the cosine of the input argument as fixed-point number in IQN format (N=1:29)

**Accuracy**  $= 20\log_2(\pi \times 2^{29}) - 20\log_2(2) = 30$  bits

**Example** The following example obtains the  $\cos(0.25 \times \pi) = 0.707$  assuming that GLOBAL\_Q is set to Q29 format in the IQmath header file.

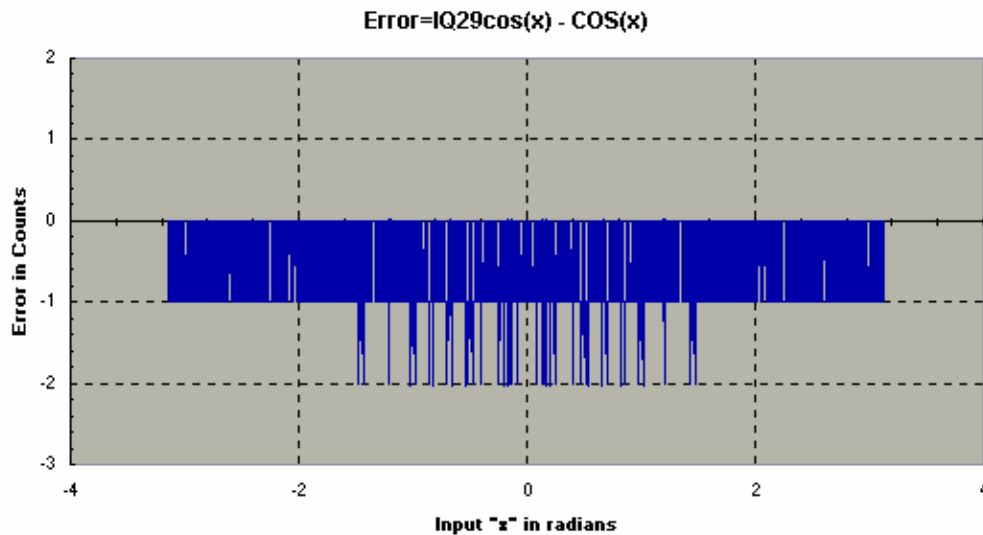
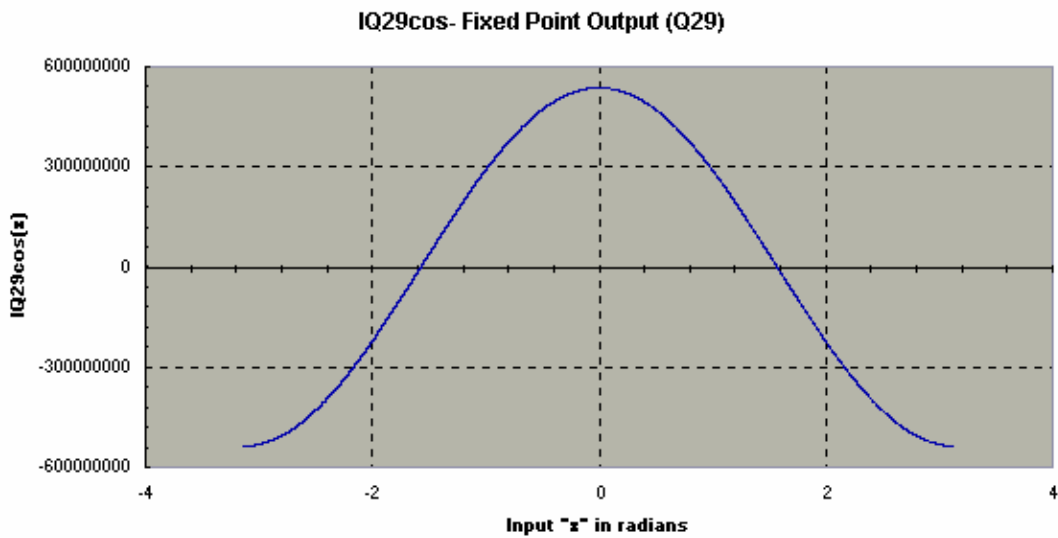
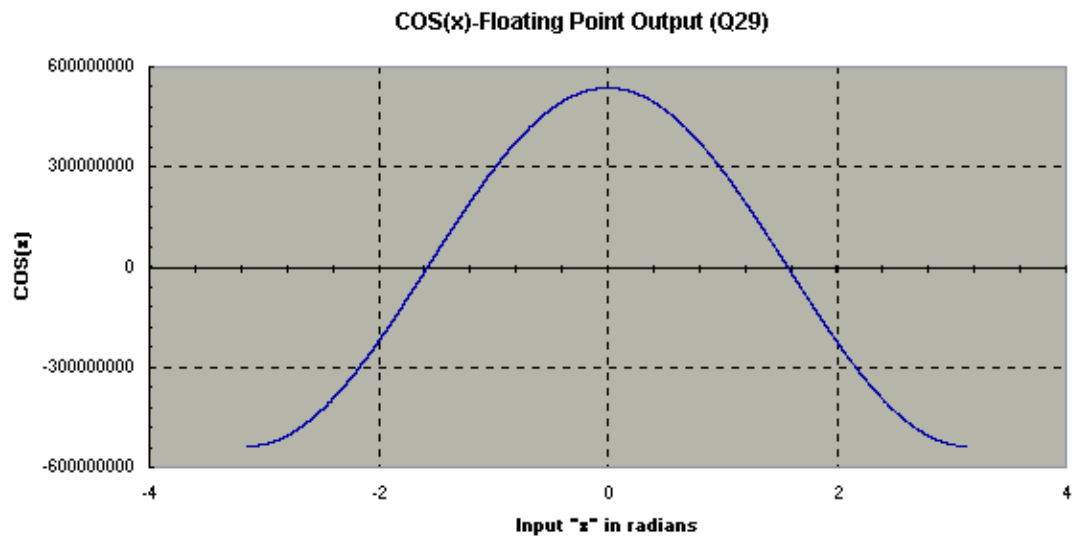
```
#include "IQmathLib.h"
#define PI 3.14156

_iq in1, out1;
_iq29 in2 out2;

void main(void ){
// in   = 0.25 x PI x 2^29 = 0x1921FB54
// out1 = cos(.25 x PI) x 2^29 = 0x16A09E66
// in   = 0.25 x PI x 2^29 = 0x1921FB54
// out1 = cos(.25 x PI) x 2^29 = 0x16A09E66

    in1  = _IQ(0.25*PI);
    out1 = _IQcos(in1);
    in2  = _IQ29(0.25*PI);
    out2 = _IQ29cos(in2);
}
```

Fixed Point COS Function vs. C Float COS: Input varies from  $-\pi$  to  $\pi$



**Description** This module computes the cosine value of the input (in per-unit radians) using table look-up and Taylor series expansion between the look up table entries.

**Declaration Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQcosPU(_iq A)
C++    iq  IQcosPU(const iq &A)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      _iqN _IQNcosPU(_iqN A)
C++    iqN IQNcosPU(const iqN &A)
```

**Input Global IQ function (IQ format = GLOBAL\_Q)**

Input argument is in per-unit radians and represented as fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Input argument is in per-unit radians and represented as fixed-point number in IQN format (N=1:30).

**Output Global IQ function (IQ format = GLOBAL\_Q)**

This function returns the sine of the input argument as fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

This function returns the sine of the input argument as fixed-point number in IQN format (N=1:30)

**Accuracy**  $= 20\log_2(1 \times 2^{30}) - 20\log_2(2) = 29$  bits

**Usage** **Example:** The following sample code obtains the  $\cos(0.25 \times \pi) = 0.707$  assuming that GLOBAL\_Q is set to Q30 format in the IQmath header file.

```
#include "IQmathLib.h"
#define PI 3.14156

_iq in1, out1;
_iq30 in2, out2

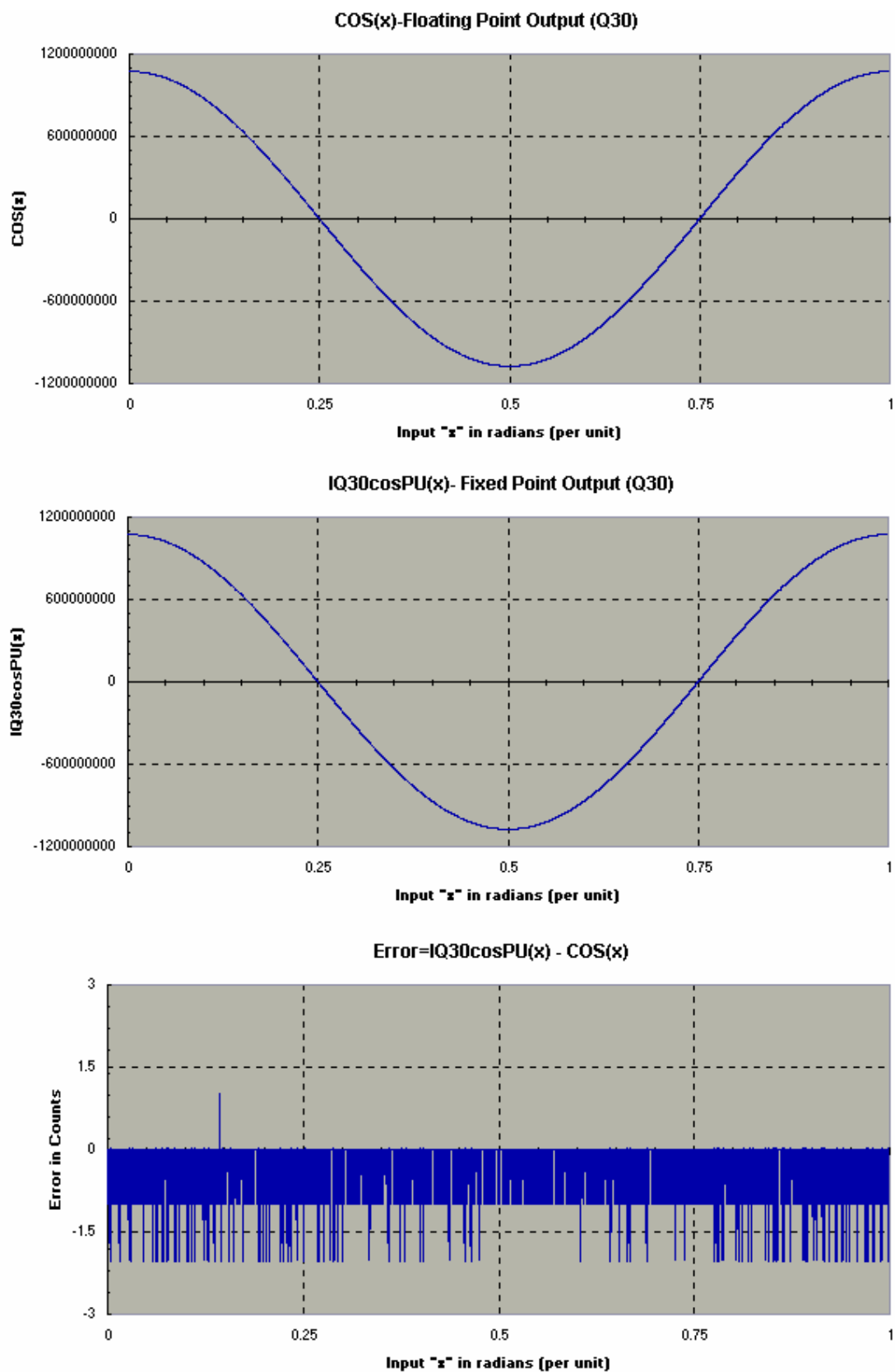
void main(void ){
// in1  = in2  = (0.25 x PI)/(2PI) x 2^30 = 0x08000000
// out1 = out2 = cos(0.25 x PI) x 2^30 = 0x2D413CCC

    in1  = _IQ(0.25*PI/PI);
    out1 = _IQcosPU(in1)

    in2  = _IQ30(0.25*PI/PI);
    out2 = _IQ30cosPU(in2);
}
```



**Fixed Point COS Function vs. C Float COS:** Input varies from 0 to  $2\pi$  in per unit



**Description** This module computes 4-quadrant arctangent. Output of this module is in radians that varies from  $-\pi$  to  $\pi$

**Declaration** **Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQatan2(_iq A, _iq B)
C++    iq  IQatan2(const iq &A, const iq &B)
```

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

```
C      _iqN _IQNatan2(_iqN A, _iqN B)
C++    iqN IQNatan2(const iqN &A, const iqN &B)
```

**Input** **Global IQ function (IQ format = GLOBAL\_Q)**

Inputs A and B are fixed-point numbers represented in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

Inputs A and B are fixed-point numbers in IQN format (N=1:29)

**Output** **Global IQ function (IQ format = GLOBAL\_Q)**

This function returns the inverse tangent of the input argument as fixed-point number in GLOBAL\_Q format. The output contains the angle in radians between  $[-\pi, +\pi]$

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

This function returns the inverse tangent of the input argument as fixed-point number in IQN format (N=1:29). The output contains the angle in radians between  $[-\pi, +\pi]$

**Accuracy**  $= 20 \log_2(\pi \times 2^{29}) - 20 \log_2(32) = 26$  bits

**Usage** The following example obtains  $\tan^{-1}(\sin(\pi/5), \cos(\pi/5)) = \pi/5$ , assuming that the GLOBAL\_Q is set to Q29 format in the IQmath header file.

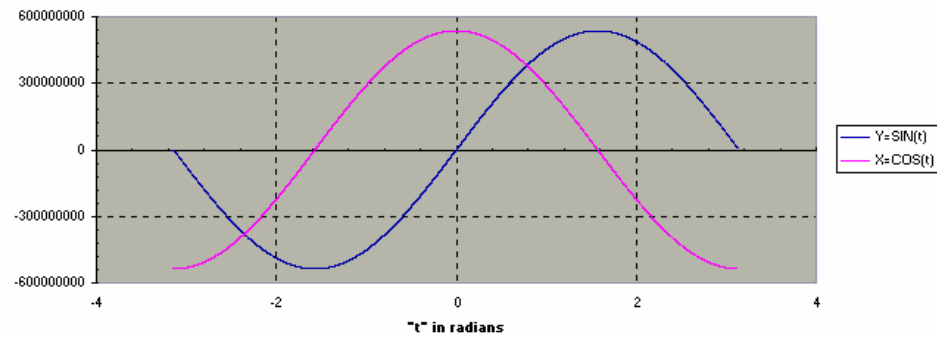
```
#include "IQmathLib.h"
#define PI 3.14156L
_iq  xin1, yin1, out1;
_iq29 xin2, yin2, out2;
void main(void ){
    // xin1 = xin2 = cos(PI/5) x 2^29 = 0x19E37FA8
    // yin1 = yin2 = sin(PI/5) x 2^29 = 0x12CF17EF
    // out1 = out2 = PI/5 x 2^29 = 0x141B21C3

    xin1 = _IQcos(_IQ(PI/5.0L));
    yin1 = _IQsin(_IQ(PI/5.0L));
    out1 = _IQatan2(yin1, xin1);

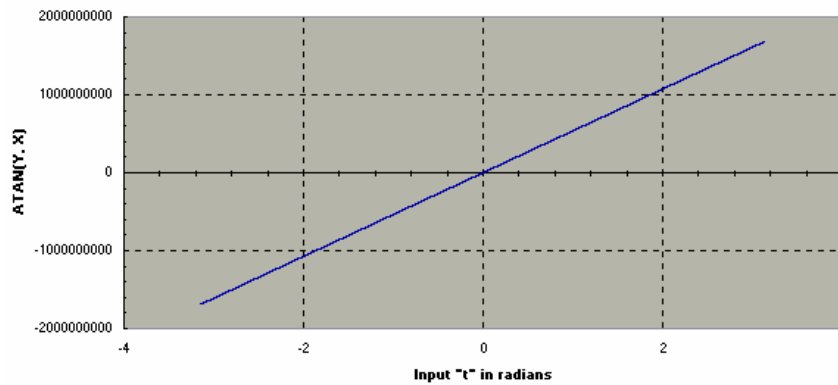
    xin2 = _IQ29cos(_IQ29(PI/5.0L));
    yin2 = _IQ29sin(_IQ29(PI/5.0L));
    out2 = _IQ29atan2(yin1, xin1);
}
```

**Fixed Point ARCTAN Function vs. C Float ARCTAN**

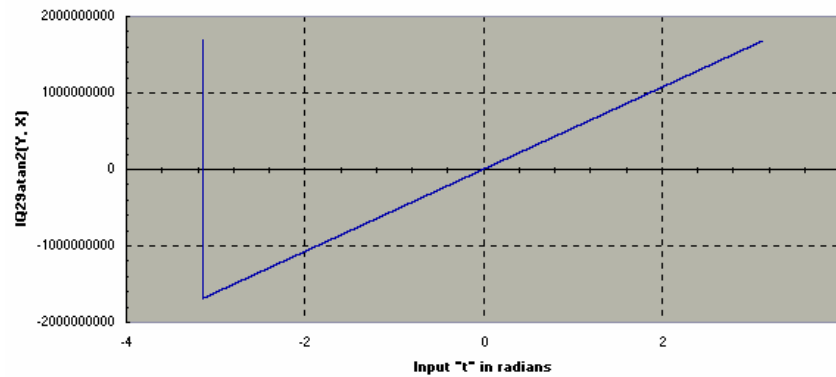
ATAN function input : Y=SIN(t) & X=COS(t) in Q29 format



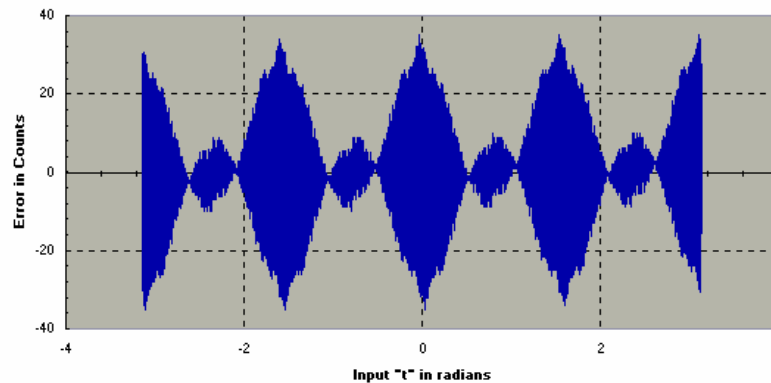
ATAN(Y, X)-Floating Point Computation (Q29)



IQ29atan2(Y, X)-Floating Point Computation(Q29)



Error=IQ29atan2(Y, X) - ATAN(Y, X)



**Description** This module computes 4-quadrant arctangent. Output of this module is in per unit radians that varies from 0 (0 radians) to 1 ( $2\pi$  radians).

**Declaration Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQatan2PU(_iq A, _iq B)
C++    iq  IQatan2PU(const iq &A, const iq &B)
```

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

```
C      _iqN _IQNatan2PU(_iqN A, _iqN B)
C++    iqN IQNatan2PU(const iqN &A, const iqN &B)
```

**Input Global IQ function (IQ format = GLOBAL\_Q)**

Inputs A and B are fixed-point number represented in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

Input A and B are fixed-point number in IQN format (N=1:29)

**Output Global IQ function (IQ format = GLOBAL\_Q)**

This function returns the inverse tangent of the input argument as fixed-point number in GLOBAL\_Q format. The output contains the angle in per unit radians that varies from 0 (0 radians) to 1 ( $2\pi$  radians).

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

This function returns the inverse tangent of the input argument as fixed-point number in IQN format (N=1:29). The output contains the angle in per unit radians that varies from 0 (0 radians) to 1 ( $2\pi$  radians).

**Accuracy**  $= 20\log_2(1 \times 2^{29}) - 20\log_2(6) = 27$  bits

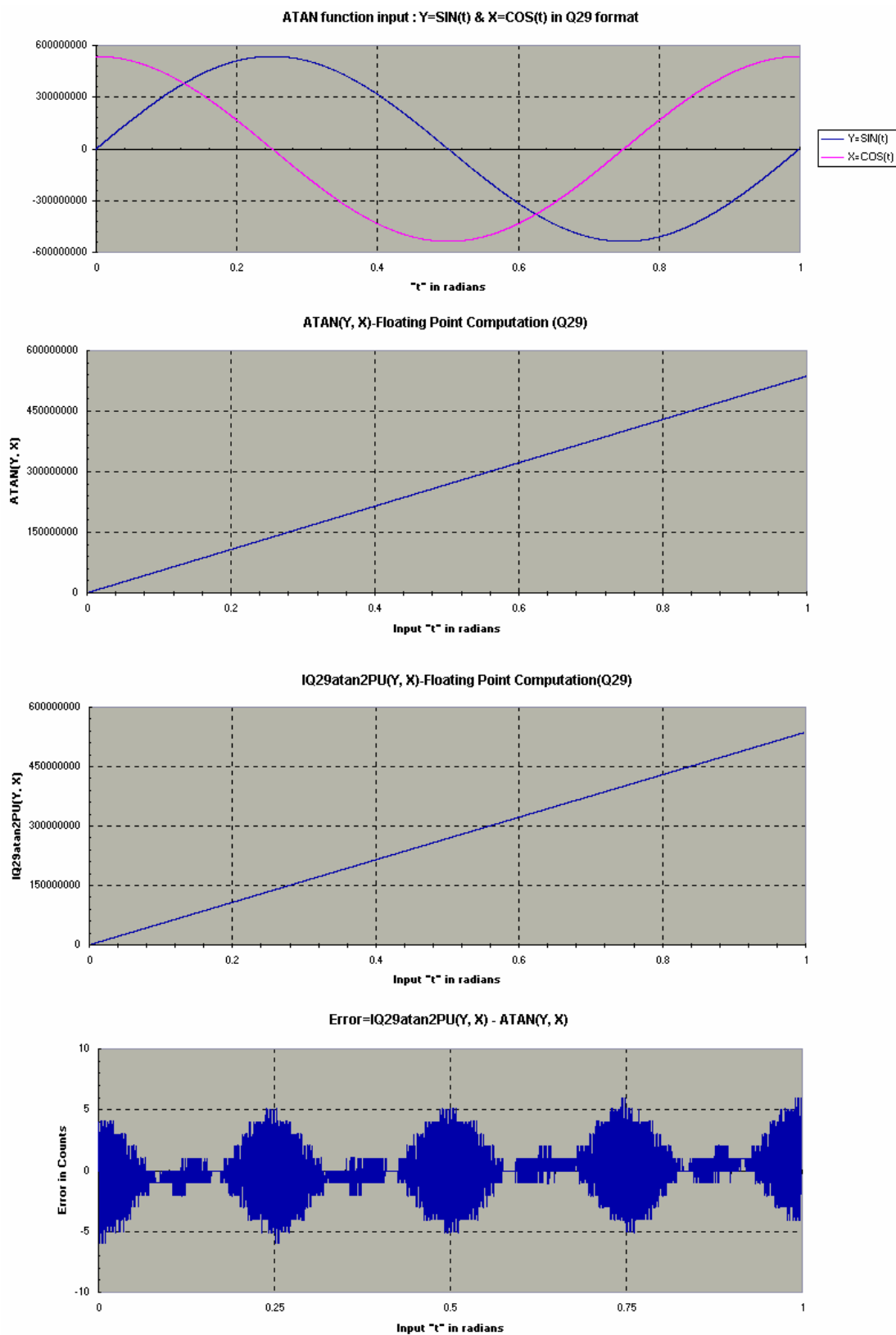
**Usage** The following sample code obtains  $\tan^{-1}(\sin(\pi/5), \cos(\pi/5)) = \pi/5$ , assuming that GLOBAL\_Q is set to Q29 format in the IQmath header file.

```
#include "IQmathLib.h"
#define PI 3.14156L
_iq  xin1, yin1, out1;
_iq29 xin2, yin2, out2;
void main(void ){
    // xin1 = xin2 = cos(PI/5) x 2^29 = 0x19E37FA8
    // yin1 = yin2 = sin(PI/5) x 2^29 = 0x12CF17EF
    // out1 = out2 = (PI/5)/(2PI) x 2^29 = 0x03333104

    xin1 = _IQcos(_IQ(PI/5.0L));
    yin1 = _IQsin(_IQ(PI/5.0L));
    out1 = _IQatan2PU(yin1, xin1);

    xin2 = _IQ29cos(_IQ29(PI/5.0L));
    yin2 = _IQ29sin(_IQ29(PI/5.0L));
    out2 = _IQ29atan2PU(yin1, xin1);
}
```

## Fixed Point ARCTAN Function vs. C Float ARCTAN



**Description** This module computes arctangent. Output of this module is in radians that vary from  $-\pi/2$  to  $\pi/2$ .

**Declaration Global IQ Macro (IQ format = GLOBAL\_Q)**

```
C      _iq _IQatan(_iq A)
C++    iq  IQatan(const iq &A)
```

**Q format specific IQ Macro (IQ format = IQ1 to IQ29)**

```
C      _iqN _IQNatan(_iqN A)
C++    iqN  IQNatan(const iqN &A)
```

**Input Global IQ function (IQ format = GLOBAL\_Q)**

Input argument is a fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

Input argument is a fixed-point number in IQN format (N=1:30)

**Output Global IQ function (IQ format = GLOBAL\_Q)**

This function returns the inverse tangent of the input argument as fixed-point number in GLOBAL\_Q format. The output contains the angle in radians between  $[-\pi/2, +\pi/2]$

**Q format specific IQ function (IQ format = IQ1 to IQ29)**

This function returns the inverse tangent of the input argument as fixed-point number in IQN format (N=1:29). The output contains the angle in radians between  $[-\pi/2, +\pi/2]$

**Accuracy**  $= 20 \log_2 \left( \frac{\pi}{2} \times 2^{29} \right) - 20 \log_2(2) = 25 \text{ bits}$

**Usage** The following example obtains  $\tan^{-1}(1) = \pi/4$ , assuming that GLOBAL\_Q is set to Q29 format in the IQmath header file.

```
#include "IQmathLib.h"
_iq in1, out1;
_iq29 in2, out2;

void main(void )
{
    in1  = _IQ(1.0L);
    out1 = _IQatan(in1);

    in2  = _IQ29(1.0L);
    out2 = _IQ29atan(in2)
}
```

## 6.4. Mathematical Utilities

### IQNexp

*Fixed point Exponential*

**Description** This module computes the exponential of a value A.

**Declaration** **Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQexp(_iq A)
C++    iq  IQexp(const iq &A)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      _iqN _IQNexp(_iqN A)
C++    iqN IQNexp(const iqN &A)
```

**Input** **Global IQ function (IQ format = GLOBAL\_Q)**

Input argument is a fixed-point number in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Input argument is a fixed-point number in IQN format (N=1:30).

**Output** **Global IQ function (IQ format = GLOBAL\_Q)**

Exponential value of the input in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Exponential value of the input in IQN format (N=1:30).

**Example** Calculate  $e(1.8) = 6.0496474$ , assuming that GLOBAL\_Q is set to Q24 format in the IQmath header file.

```
#include "IQmathLib.h"
_iq in1, out1;
_iq30 in2, out2;

void main(void )
{
    // in1  = in2  = 1.8 x 2^24 = 0x01CCCCC
    // out1 = out2 = exp(1.8) x 2^24 = 0x060CB5AA

    in1  = _IQ(1.8);
    out1 = _IQexp(x);

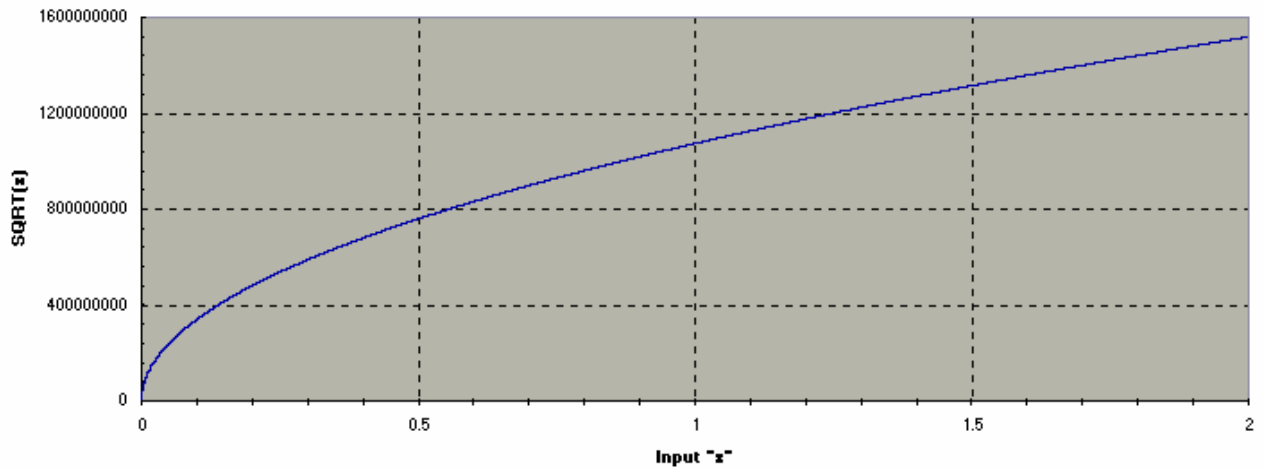
    in2  = _IQ24(1.8);
    out2 = _IQ24exp(x);
}
```

<b>Description</b>	This module computes the square root of the input using table lookup and Newton-Raphson approximation.
<b>Declaration</b>	<p><b>Global IQ function (IQ format = GLOBAL_Q)</b></p> <pre>C      _iq _IQsqrt(_iq A) C++    iq  IQsqrt(const iq &amp;A)</pre> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ30)</b></p> <pre>C      _iqN _IQNsqrt(_iqN A) C++    iqN IQNsqrt(const iqN &amp;A)</pre>
<b>Input</b>	<p><b>Global IQ function (IQ format = GLOBAL_Q)</b> Input argument is a fixed-point number in GLOBAL_Q format.</p> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ30)</b> Input argument is a fixed-point number in IQN format (N=1:30)</p>
<b>Output</b>	<p><b>Global IQ function (IQ format = GLOBAL_Q)</b> Square root of input in GLOBAL_Q format.</p> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ30)</b> Square root of input in IQN format (N=1:30)</p>
<b>Accuracy</b>	$= 20\log_2(2^{31}) - 20\log_2(6) = 29$ bits
<b>Usage</b>	<p>Calculate <math>\sqrt{1.8} = 1.34164</math>, assuming that GLOBAL_Q is set to Q30 format in IQmath header file.</p> <pre>#include "IQmathLib.h" _iq in1, out1; _iq30 in2, out2;  void main(void ) {     // in1  = in2  = 1.8 x 2^30 = 0x73333333     // out1 = out2 = sqrt(1.8) x 2^30 = 0x55DD7151      in1  = _IQ(1.8);     out1 = _IQsqrt(x);      in2  = _IQ30(1.8);     out2 = _IQ30sqrt(x); }</pre>

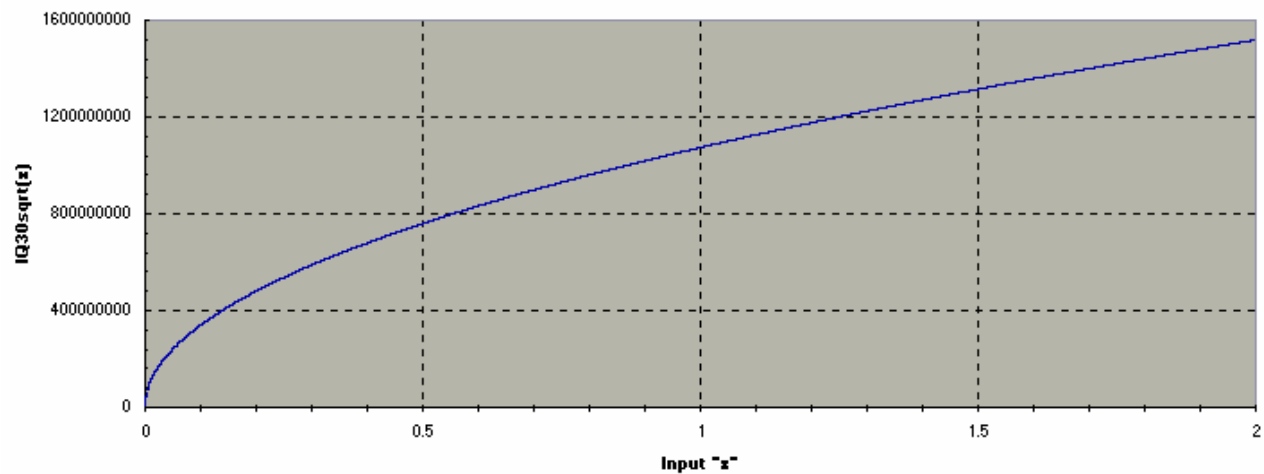


**Fixed Point SQRT Function vs. C Float SQRT**

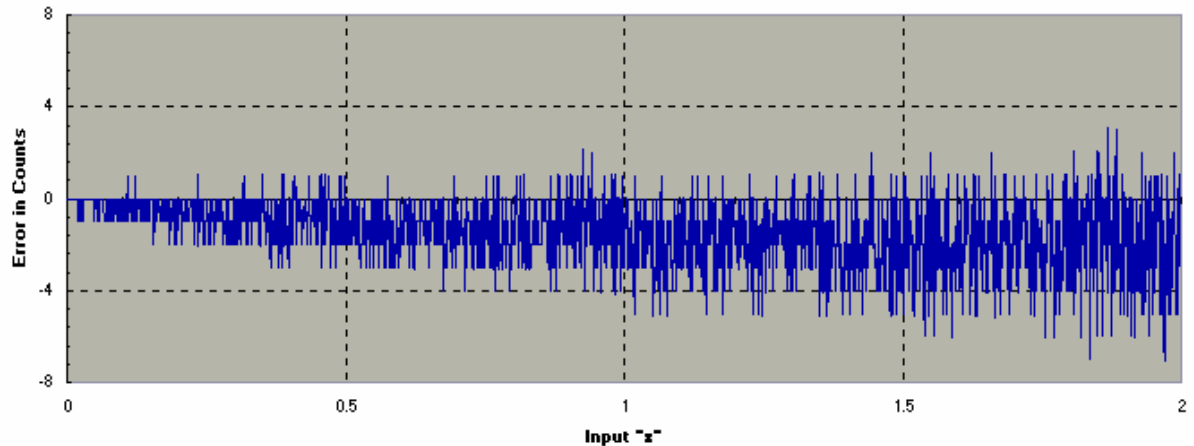
**SQRT(x)-Floating Point Computation (Q30)**



**IQ30sqrt(x)-Floating Point Computation (Q30)**



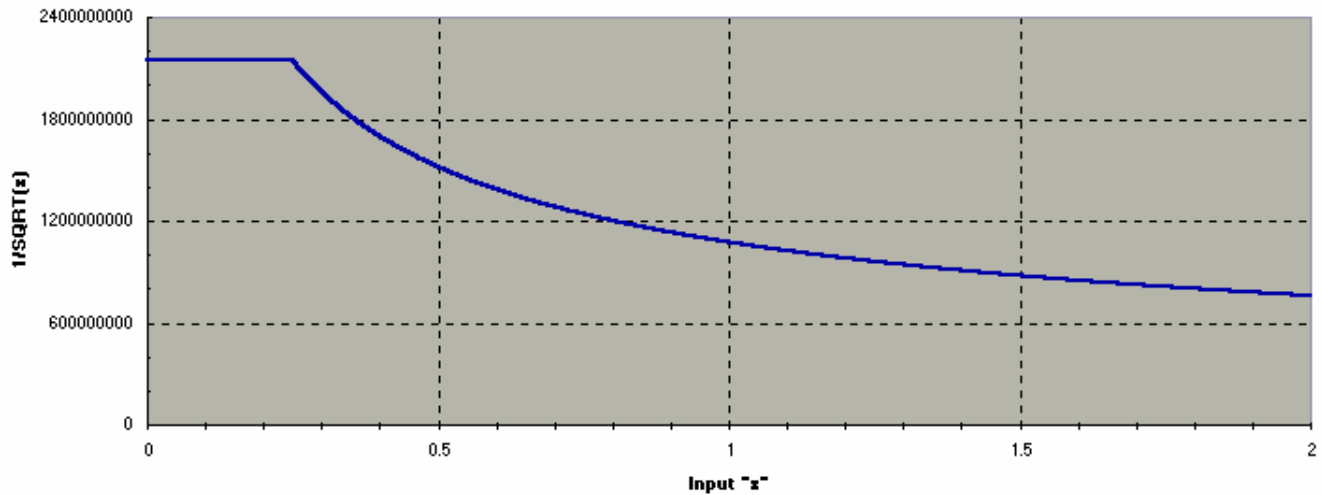
**Error=IQ30sqrt(x)-SQRT(x)**



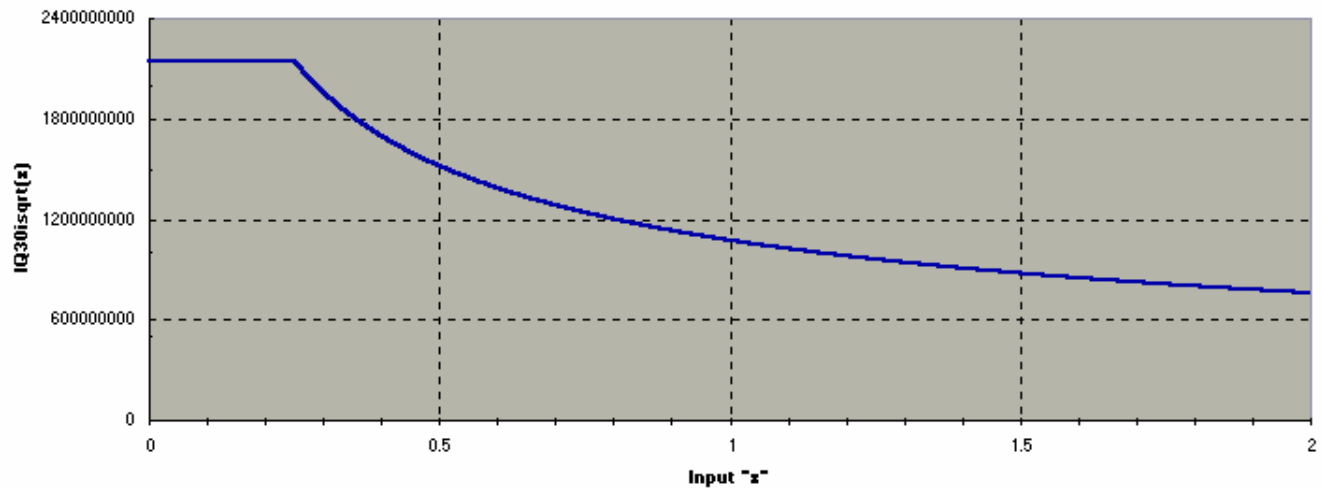
<b>Description</b>	This module computes the inverse square root of the input using table lookup and Newton-Raphson approximation.
<b>Declaration</b>	<p><b>Global IQ function (IQ format = GLOBAL_Q)</b></p> <pre>C      _iq _IQisqrt(_iq A) C++    iq  IQisqrt(const iq &amp;A)</pre> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ30)</b></p> <pre>C      _iqN _IQNisqrt(_iqN A) C++    iqN IQNisqrt(const iqN &amp;A)</pre>
<b>Input</b>	<p><b>Global IQ function (IQ format = GLOBAL_Q)</b> Input argument is a fixed-point number in GLOBAL_Q format.</p> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ30)</b> Input argument is a fixed-point number in IQN format (N=1:30)</p>
<b>Output</b>	<p><b>Global IQ function (IQ format = GLOBAL_Q)</b> Inverse square-root of the input expressed in GLOBAL_Q format.</p> <p><b>Q format specific IQ function (IQ format = IQ1 to IQ30)</b> Inverse square root of input expressed in IQN format (N=1:30)</p>
<b>Accuracy</b>	$= 20\log_2(2^{31}) - 20\log_2(5) = 29$ bits
<b>Usage</b>	<p>Calculate <math>\frac{1}{\sqrt{1.8}} = 0.74535</math> assuming that GLOBAL_Q is set to Q30 format in the IQmath header file.</p> <pre>#include "IQmathLib.h"  _iq in1, out1; _iq30 in2, out2;  void main(void ) {     // in1  = in2  = 1.8 x 2^30 = 0x73333333     // out1 = out2 = 1/sqrt(1.8) x 2^30 = 0x2FB3E99E      in1  = _IQ(1.8);     out1 = _IQisqrt(in1);      in2  = _IQ30(1.8);     out2 = _IQ30isqrt(in2); }</pre>

## Fixed Point inverse SQRT Function vs. C Float inverse SQRT

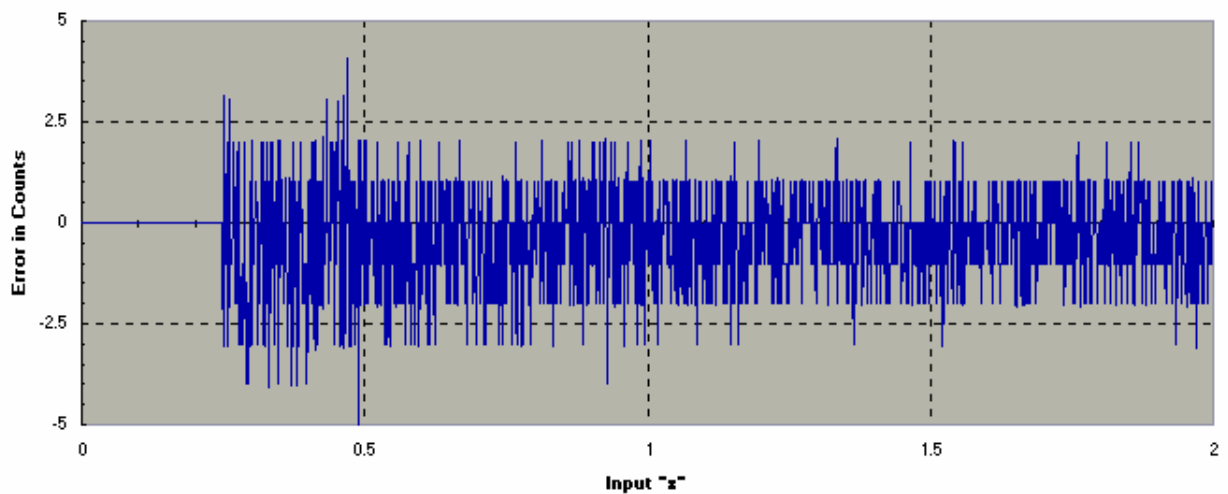
1/SQRT(x)-Floating Point Computation (Q30)



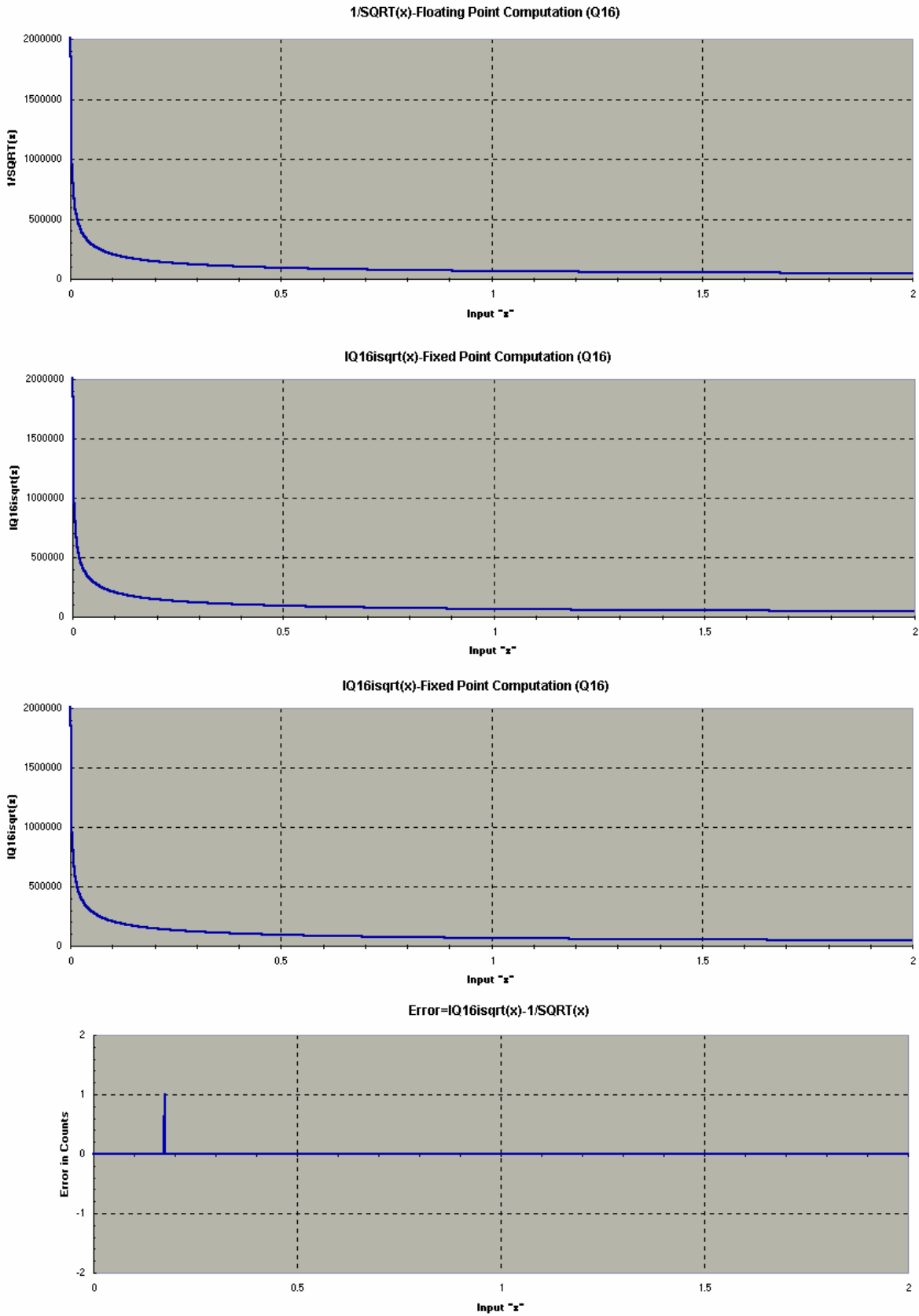
IQ30isqrt(x)-Fixed Point Computation (Q30)



Error=IQ30isqrt(x)-1/SQRT(x)



Fixed Point inverse SQRT Function vs. C Float inverse SQRT



**Description** This function calculates the magnitude of two orthogonal vectors as follows:  $Mag = \sqrt{A^2 + B^2}$ . This operation achieves better accuracy and avoids overflow problems that may be encountered by using the "\_IQsqrt" function.

**Declaration** **Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQmag(_iq A, _iq B)
C++    iq  IQmag(const iq &A, const iq &B)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      _iqN _IQNmag(_iqN A, _iqN B)
C++    iqN IQNmag(const iqN &A, const iqN &B)
```

**Input** **Global IQ function (IQ format = GLOBAL\_Q)**

Inputs A and B are IQ numbers represented in GLOBAL\_Q format.

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Inputs A and B are IQ numbers represented in IQN format

**Output** **Global IQ function (IQ format = GLOBAL\_Q)**

Magnitude of the input vector in GLOBAL\_Q format

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Magnitude of the input vector in IQN format

**Accuracy** 29-bits (Same as SQRT function)

**Usage** **Example:**

The following sample code obtains the magnitude of the complex number (Assuming GLOBAL\_Q=IQ28).

```
#include "IQmathLib.h"
// Complex number = real1 + j*imag1
// Complex number = real2 + j*imag2

_iq real1, imag1, mag1;
_iq28 real2, imag2, mag2;

void main(void )
{

// mag1 = 5.6568 in IQ28 format
real1 = _IQ(4.0);
imag1 = _IQ(4.0);
mag1 = _IQmag(real1, imag1);

// mag2 = ~8.0, saturated to MAX value (IQ28)!!!
real2 = _IQ28(7.0);
imag2 = _IQ28(7.0);
mag2 = _IQ28mag(real2, imag2);

}
```

## 6.5. Miscellaneous Utilities

<b>IQNabs</b>	<i>Absolute value of IQ number</i>
---------------	------------------------------------

**Description** This intrinsic calculates the absolute value of an IQ number.

**Declaration** **Global IQ function (IQ format = GLOBAL\_Q)**

```
C      _iq _IQabs(_iq A)
C++    iq  IQabs(const iq &A)
```

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

```
C      _iqN _IQNabs(_iqN A)
C++    iqN IQNabs(const iqN &A)
```

**Input** **Global IQ function (IQ format = GLOBAL\_Q)**

IQ number in GLOBAL\_Q format

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

IQ number in IQN format

**Output** **Global IQ function (IQ format = GLOBAL\_Q)**

Absolute value of input in GLOBAL\_Q format

**Q format specific IQ function (IQ format = IQ1 to IQ30)**

Absolute value of input in IQN format

**Usage** **Example:**

Calculate the absolute sum of three IQ numbers assuming GLOBAL\_Q=IQ28 in the IQmath header file.

```
#include "IQmathLib.h"

void main(void)
{
    _iq xin1, xin2, xin3, xsum;
    _iq20 yin1, yin2, yin3, ysum;

    xsum = _IQabs(X0) + _IQabs(X1) + _IQabs(X2);
    xsum = _IQ28abs(X0) + _IQ28abs(X1) + _IQ28abs(X2);
}
```

**Description** This intrinsic saturates an IQ value to the given Positive and Negative limits. This operation is useful in areas where there is potential for overflow in a calculation.

**Declaration** `_iq _IQsat(_iq A, long P, long N)`

**Input** **Global IQ function (IQ format = GLOBAL\_Q)**  
IQ number in GLOBAL\_Q format

**Output Format Global IQ function (IQ format = GLOBAL\_Q)**  
Saturated output in GLOBAL\_Q format

**Usage** **Example:**

Calculate the linear equation " $Y = M * X + B$ ", with saturation.

All variables are GLOBAL\_Q = 26. However, there is a possibility that the variable ranges may cause overflow, so we must perform the calculation and saturate the result.

To do this, we perform the intermediate operations using IQ = 20 and then saturate before converting the result back to the appropriate GLOBAL\_Q value:

```
#include "IQmathLib.h

void main(void)
{
    _iq Y, M, X, B;           // GLOBAL_Q = 26 (+/- 32 range)
    _iq20 temp;               // IQ = 20 (+/- 2048 range)

    temp = _IQ20mpy(_IQtoIQ20(M), _IQtoIQ20(X)) +
           _IQtoIQ20(B);
    temp = _IQsat(temp, _IQtoIQ20(MAX_IQ_POS),
                  _IQtoIQ20(MAX_IQ_NEG));

    Y = _IQ20toIQ(temp);
}
```

## Chapter 7. Revision History

Version	Date	Comment
V1.5	July 8, 2008	<p>Added IQNtoa.</p> <p>Header IQmathLib.h and IQmathCPP.h files were updated to fix typos and missing information. Refer to the header files themselves for more information.</p> <p>Added a version of the library built with the compiler switch <code>--float_support=fpu32</code>. This enables mixing the IQmath with the native floating support capabilities of C28x+FPU.</p> <p>Added information describing how to convert between IQmath and float math.</p> <p>Added the IQexp, IQasin, IQacos, and IQNtoa function information to this document.</p> <p>Added C++ information to this document. Previously this information was only in a readme.txt file.</p> <p>Added information regarding locations of tables stored in the boot ROM of different devices.</p> <p>Noted the IQmath .gel file is most useful when using a legacy debugger that does not support IQmath.</p> <p>Added examples for 2808, 28335 and 28235. Updated the example flow to better match the header file and peripheral examples also provided by TI.</p> <p>General documentation cleanup and improvements.</p> <p>Install is now under a version specific directory. Changed the directory structure to reduce the number of duplicated files.</p>
V1.4f	March 10, 2005	Fixed bug in IQexp.
V1.4e	June 17, 2004	Added IQexp, IQasin, IQacos.
V1.4d	March 30, 2003	Previous Web Release